

Re-Engineering Approach for PLC Programs based on Formal Methods

Mohammed Bani Younis

- Introduction
- Re-Engineering of PLC Programs
- Formalization of PLC Programs
- Visualization of the formalized PLC Programs
- Re-Implementation of PLC Programs
- SW-Quality
- Case Studies
- Summary

Introduction

Re-Engineering

Formalization

Visualization

Re-Implem.

SW-Quality

Case Stud.

Summary

- Programmable Logic Controllers (PLCs)
 - Special type of computers used in industrial and safety applications
 - System controlled by PLC programs vary in complexity
- Programming Languages (IEC 61131-3):
 - *Ladder Diagram (LD)*
 - *Instruction List (IL)*
 - *Function Block Diagram (FBD)*
 - *Structured Text (ST)*
 - *Sequential Function Chart (SFC)*
 - *However, also vendor-specific languages*

Introduction

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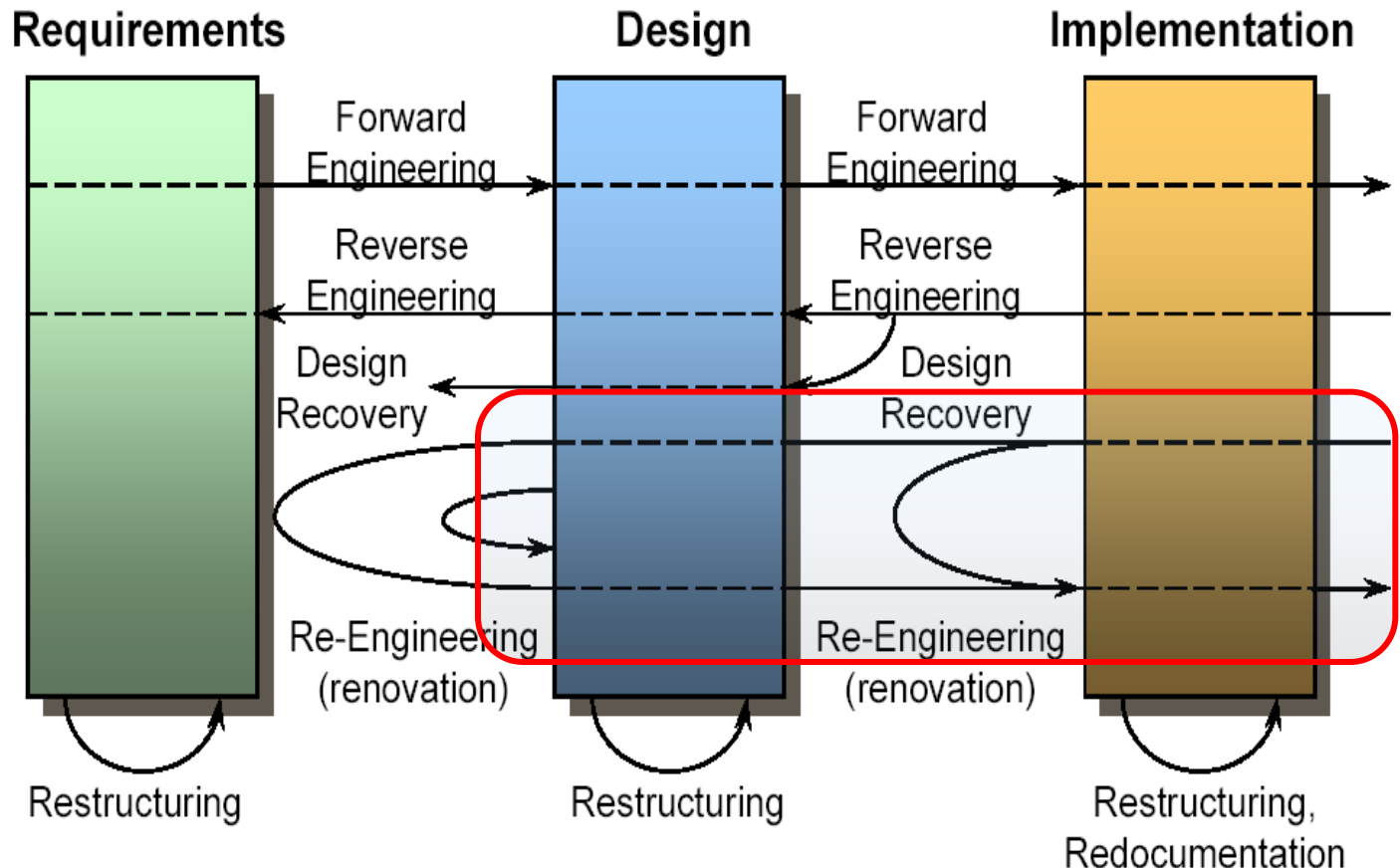
Visualization

Re-Implem.

SW-Quality

Case Stud.

Summary



[Chikofsky and Cross 1990]

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Summary

- Longevity of PLC programs (often more than 30 years)
 - Problems with HW
 - code is HW-specific
 - replacement to a new HW problematic
 - replacement of the supplier problematic
 - ⊕ e.g.: Siemens S5 is no more produced, Siemens S7 can not process S5 programs

Goals

- Code is continuously adjusted → documentation problems
 - no formal description at the beginning
 - undocumented adjustments
 - ⊕ Need for visualization
- New Technologies hold move in the area of Automation
 - better SW-Engineering methods
 - short HW-Life cycles
 - ⊕ Formal model allows adjustments on new HW-SW environment

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Summary

- Convert STEP 5 → STEP 7 (**Siemens Automation and Drives TIA**)
 - Not all Program Constructs (e.g. Standard functions)
 - Often with simplifications are used
 - Delete non Compatible Blocks and invocations
 - These should be re-programmed in STEP 7
 - Programs of normal instruction are converted easily and complete Addressing

→ Logical dynamic is not converted

- STEP 5 → IEC 61131-3 (**3S CodeSys**)
 - Import .SYM
 - standard.lib to the project
 - SEQ-file as Global Variables of the IEC 61131-3
 - The Address is matched to the IEC 61131-3
 - Non-Valid Characters and Functions are comment out

→ only Instruction mapping (no Logic)

Reference	Classification				
	Source		Level	Aim	Model
	Lang.	Additional			
[Storr and Kraneis, 1997]	IL	Plant	Program	Re-Eng.	Automaton
[Treseler et al., 2000]	IL	Plant	Program	Verification	Automaton
[Bornot et al., 2000 (b)]	SFC	Without	Program	Verification	SMV Input Code
[Willems, 1999]	IL	Plant	Program	Verification	Timed Automaton
[Mader and Wupper, 1999]	IL	Without	Algorithm	Verification	Timed Automaton
[Brinksma and Mader, 2000]	SFC	Plant	Program	Verification	SPIN model
[Kowalewski et al., 1999]	SFC	Plant	Program	Static analysis	Automaton
[Bornot et al., 2000 (a)]	IL	Without	Program	Verification	No model
[Canet et al., 2000]	IL	Without	Program	Verification	Automaton
[Roussel and Lesage, 1996]	SFC	Without	Program	Verification	FSM
[Lampérière-Couffin et al., 1999]	SFC&LD	Without	Program	Verification	Automaton
[Mertke and Menzel, 2000]	IL	Plant	Program	Verification	PN
[Hassapis et al., 1998]	SFC	Plant	Program	Verification	hybrid Automaton
[Rossi and Schnoebelen, 2000]	LD	Without	Program	Verification	FSM
[Baresi et al., 2000]	FBD	Without	Algorithm	Verification	PN
[Hatono and Baba, 1996]	LD	Without	Program	Verification	PN
[Vyatkin and Hanisch, 2000]	FBD	Plant	Program	Verification	SNS
[Canet, 2001]	ST	Without	Algorithm	Verification	Automata

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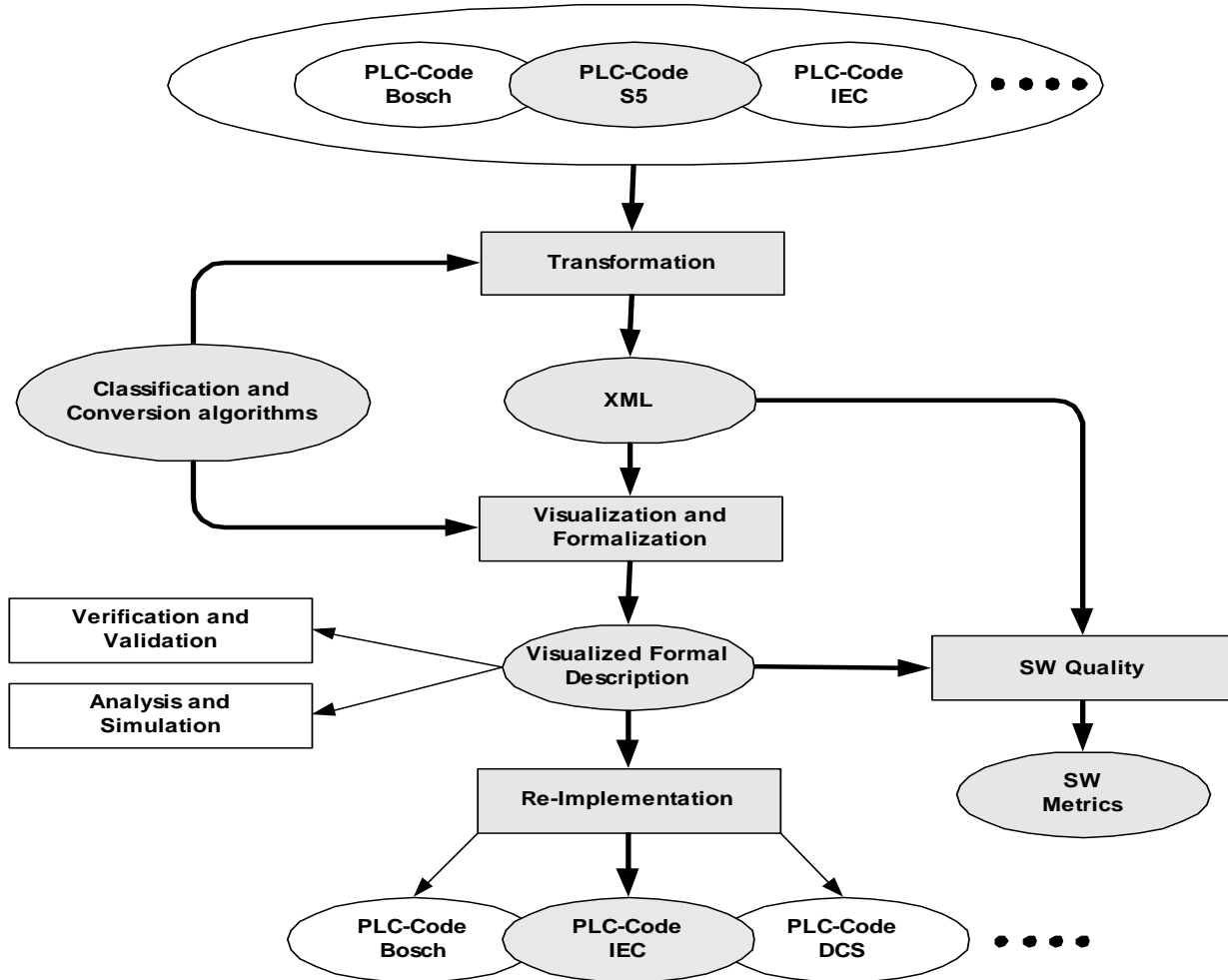
Case Stud.

Summary

- **Internet and OO Re-Engineering**
 - New trend in controller design
 - Majority of the works are Forward Engineering
 - Evaluation of OOP delegated through Unified Modeling Language (UML)
 - Use of UML as modeling environment
 - Use of Internet Technologies (XML, HTML, XSL, etc...)

→ Research against Industry

- Compound of OO, Internet, and formal methods



Done

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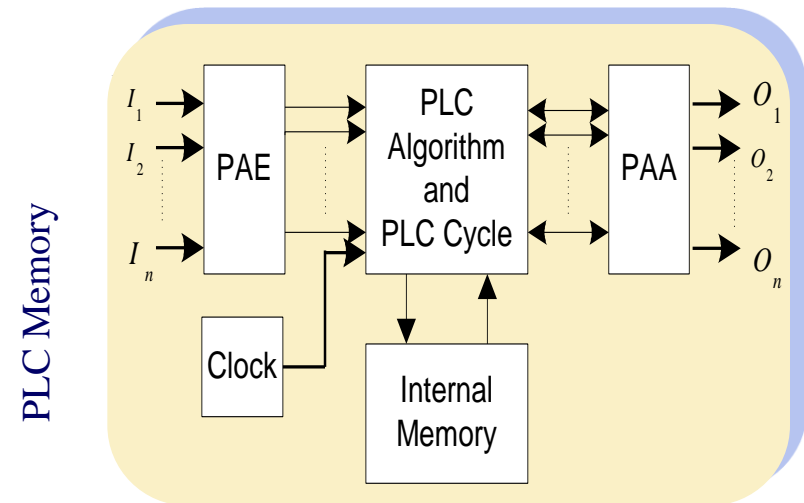
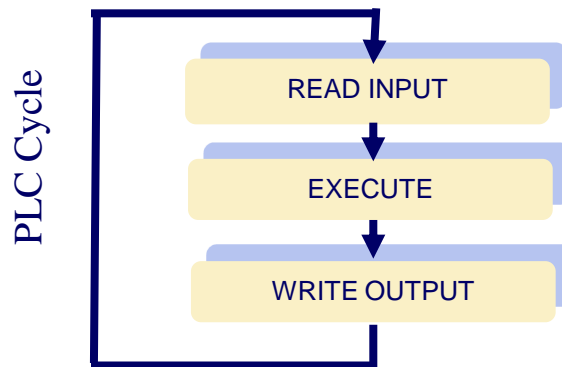
Re-Implem.

SW-Quality

Case Stud.

Summary

- STEP 5 in a hierarchy-like form:
 - *OB*: Organization Module
 - *PB*: Program Module
 - *DB*: Data Module
 - *FB*: Function Module
- Timers and Counters
- Polling mode operation
- PLC Memory



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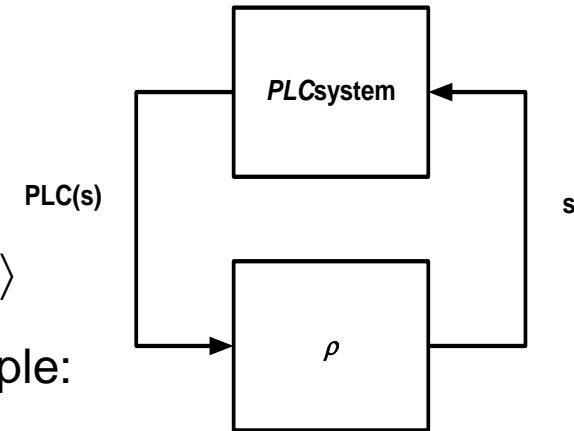
Re-Implem.

SW-Quality

Case Stud.

Summary

- $PLC_{system}/\rho \rightarrow$ closed loop
- plant as a FSM: $\rho = \langle S, \Sigma, X_0, X_f, \delta \rangle$
- PLC_{system} as a tuple $\langle PLC_{SW}, PLC_{HW}, PLC_{Cycle} \rangle$
- PLC_{SW} which denotes the PLC program as tuple:
 $\langle PAE, PAA, I, A_{PAE}, PLC_{pr}, x_0, x_f \rangle$
- PLC_M module or block as a stand alone is a tuple: $\langle S, \Sigma, Y, \delta, \lambda, s_0, s_f \rangle$
- S set of states
- $Y = \alpha(PAA)$ output alphabet
- $\delta: S \times \Sigma \rightarrow S$ transition function
- $\Sigma = \alpha(PAE)$ input alphabet
- $\lambda: S \times \Sigma \rightarrow Y$ output function



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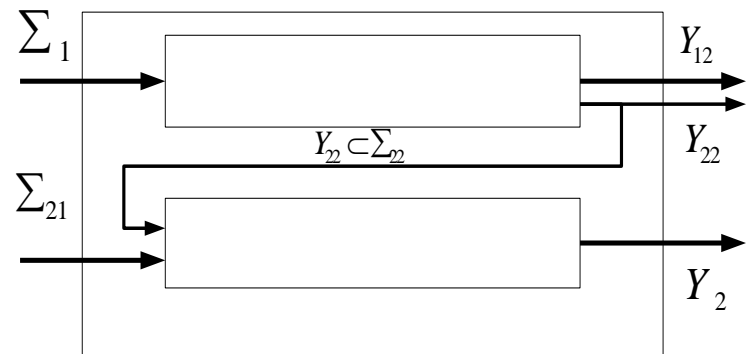
SW-Quality

Case Stud.

Summary

- PLC_{SW} is a two subsets PLC_U and PLC_{SYS}
- PLC_U is re-engineering relevant
- PLC_U is a model of CFSM $PLC_{M1} \dots PLC_{Mn}$ of $\langle S_i, \Sigma_i, Y_i, \delta_i, \lambda_i, s_{0,i} \rangle$
- The model $PLC_{Mi} \forall i \in \{1, \dots, n\} PLC_{M1} \otimes PLC_{M2} \otimes \dots \otimes PLC_{Mn}$ builds the automaton $PLC_U := \langle S, \Sigma, Y, \delta, \lambda, s_0 \rangle$

General feed-forward composition



$$Y_i = Y_{i1} \times Y_{i2}$$

$$\Sigma_i = \Sigma_{i1} \times \Sigma_{i2}$$

PLC Program and Cycle

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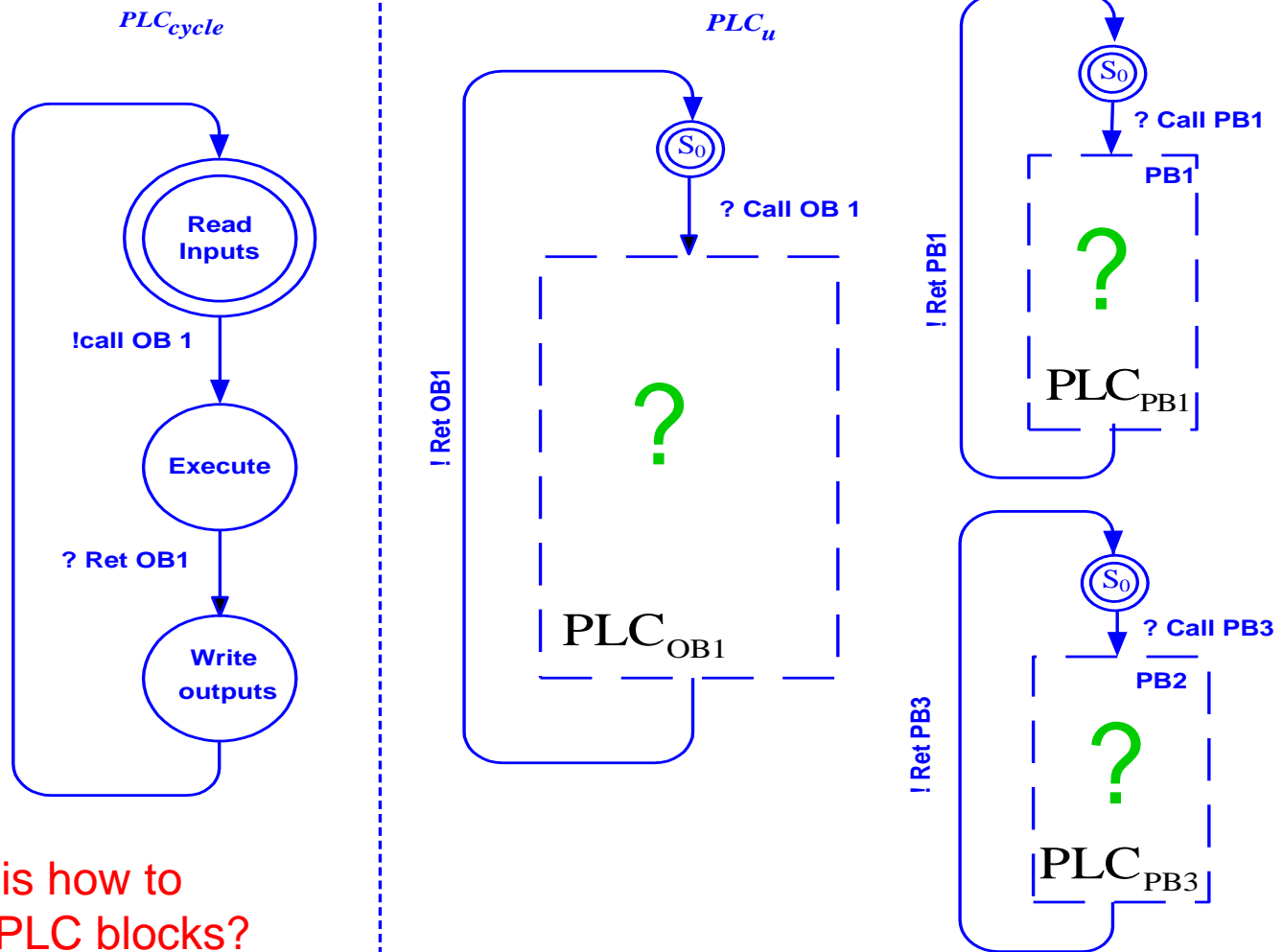
Re-Implem.

SW-Quality

Case Stud.

Summary

- PLC_{Cycle} as CFSM with the CFSMs of PLC_u
- Example $PLC_{OB1} \otimes PLC_{PB1} \otimes PLC_{PB3}$



Next step is how to formalize PLC blocks?

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Summary

- State definition through the influence of single operations
- Investigation of the operations on the Status Word

- Status Word
- CR (VKE in German)

Different possibilities were examined

1. All possibilities of a single operation are concerned \rightarrow State = f (VKE, PC, internal variables)
2. the conversion of the program according to University of Cachan \rightarrow Q is the set of states and is a tuple (V, a, m), V: variables, a: accumulator, m: program counter
3. Optimization of 2, operation of the same type are merged to form a coherent segment
4. IF-THEN-ELSE transformation \rightarrow State = f (PC, variables)
5. Conversion to Moore machine
6. Based on 4, no need for state contents

PLC Text Example:

```

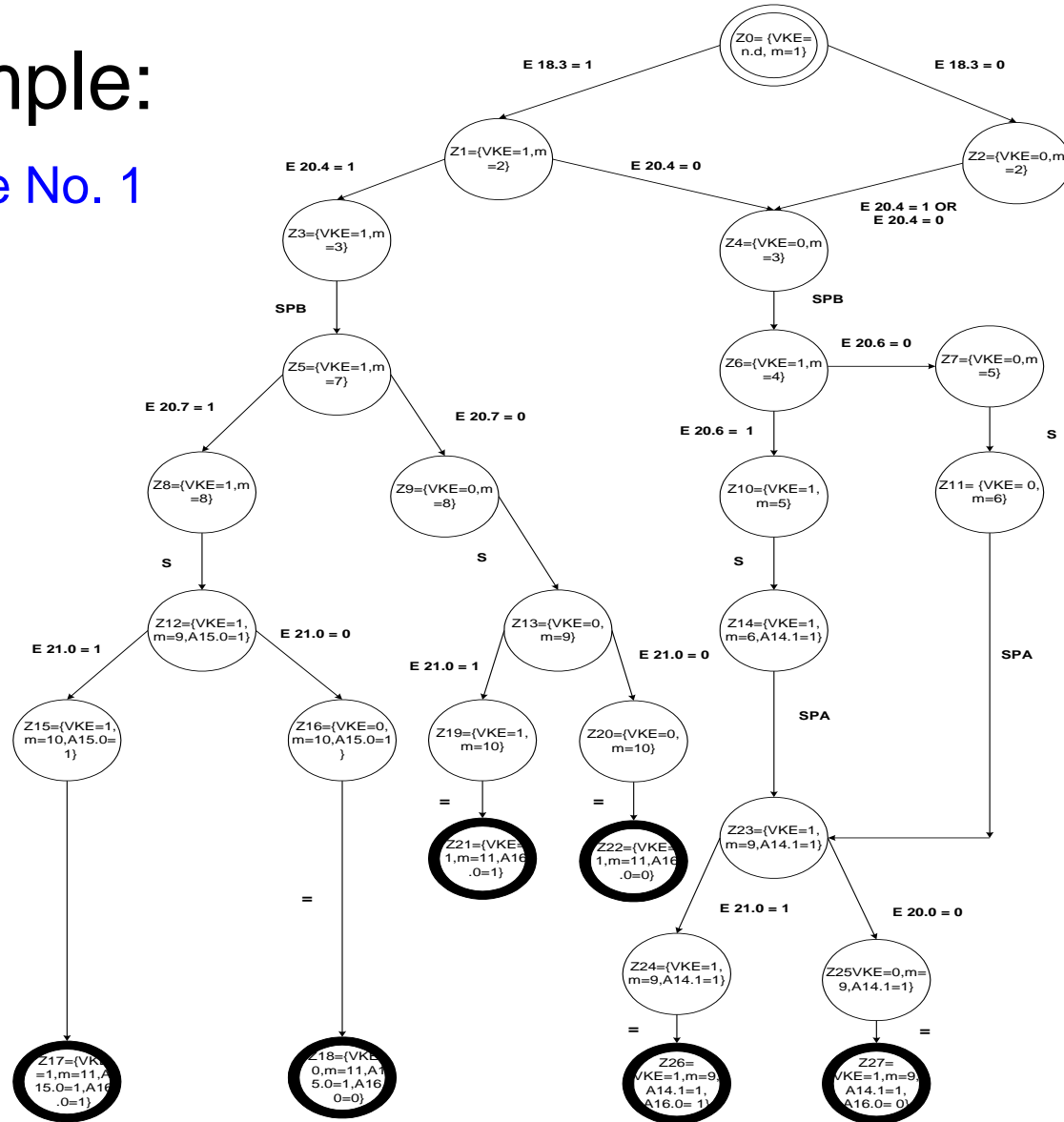
Kommentar :
Autor      :
Erstellt   :15.07.2003   Geändert am:
              BIB:0

NETZWERK   1
0000              :U      E      38.1
0001              :U      E      18.3
0002              :U      E      20.4
0003              :SPB    LAB1
0004              :U      E      20.6
0005              :S      A      14.1
0006              :SPA    LAB2
0007      LAB1    :U      E      20.7
0008              :=      A      15.0
0009      LAB2    :O      E      21.0
000A              :=      A      16.0
000B              :BE

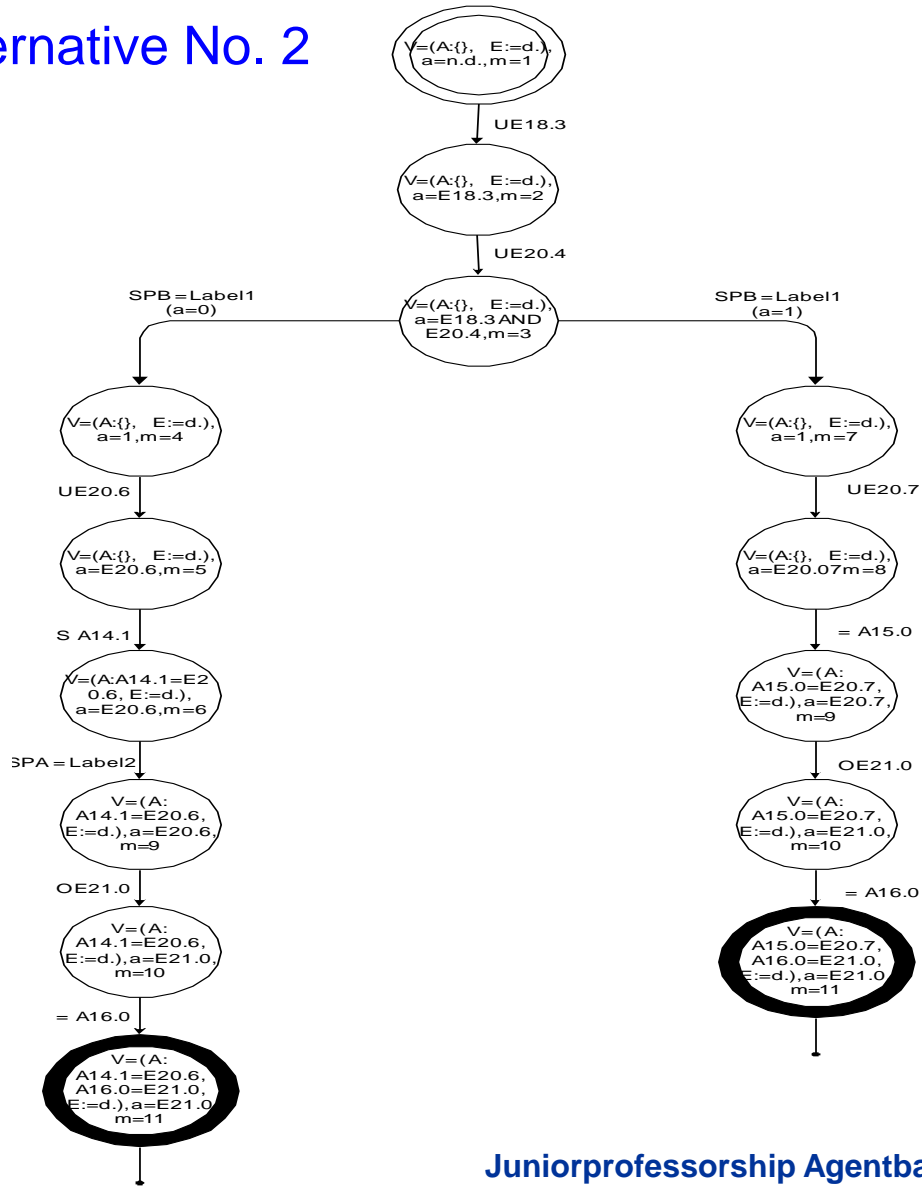
```

Example:

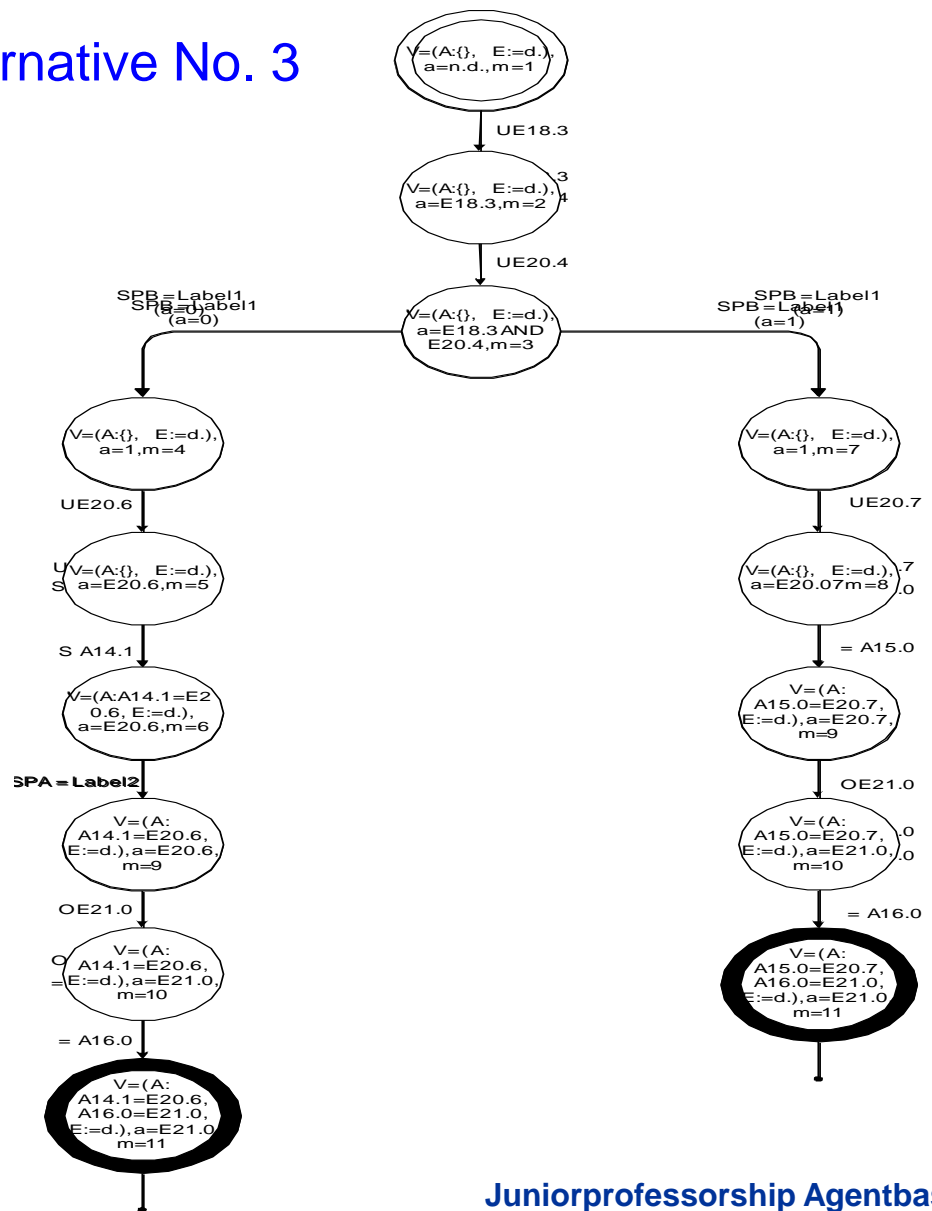
Alternative No. 1



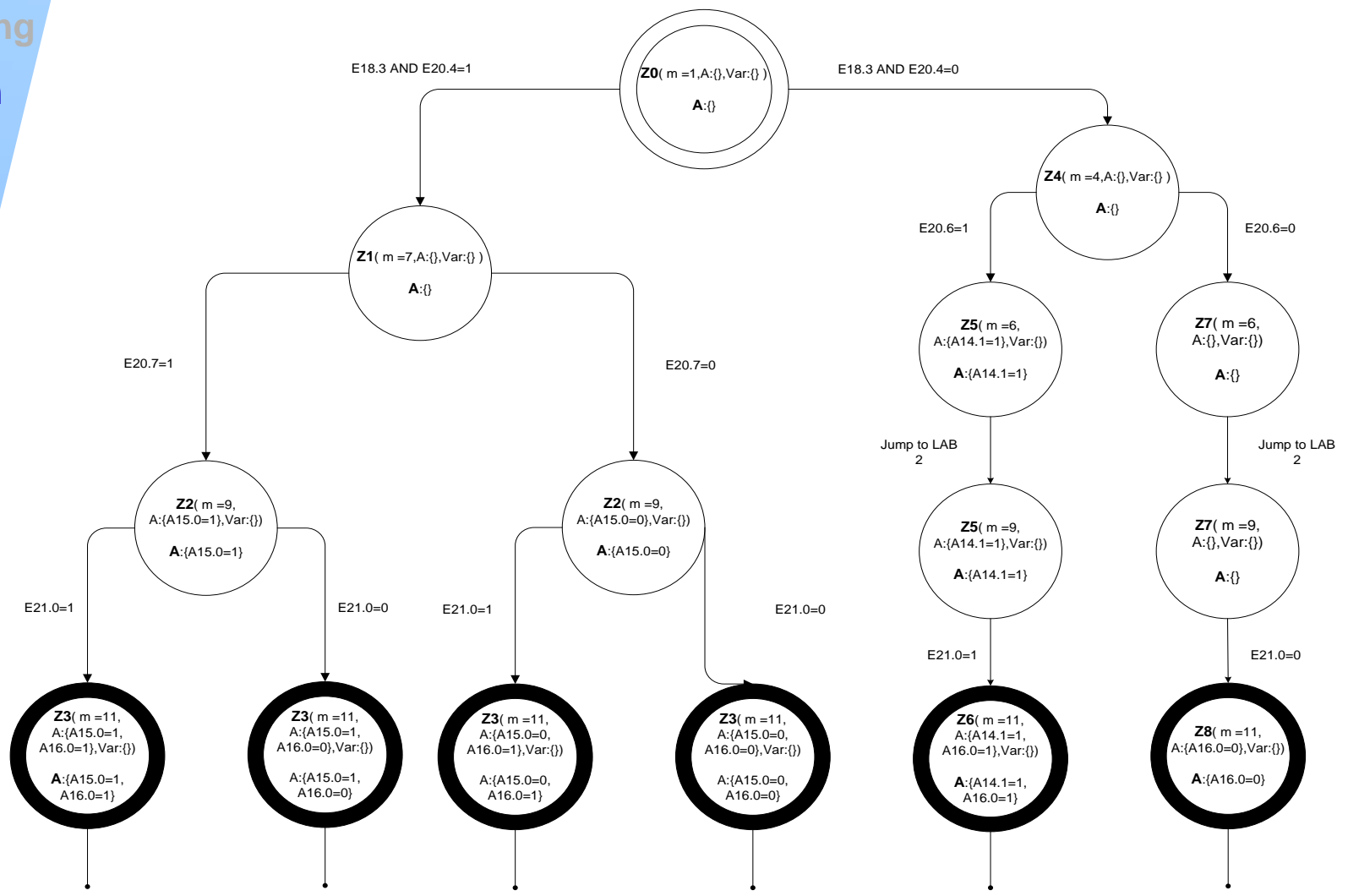
Alternative No. 2



Alternative No. 3



Alternative No. 5



PLC Text

```

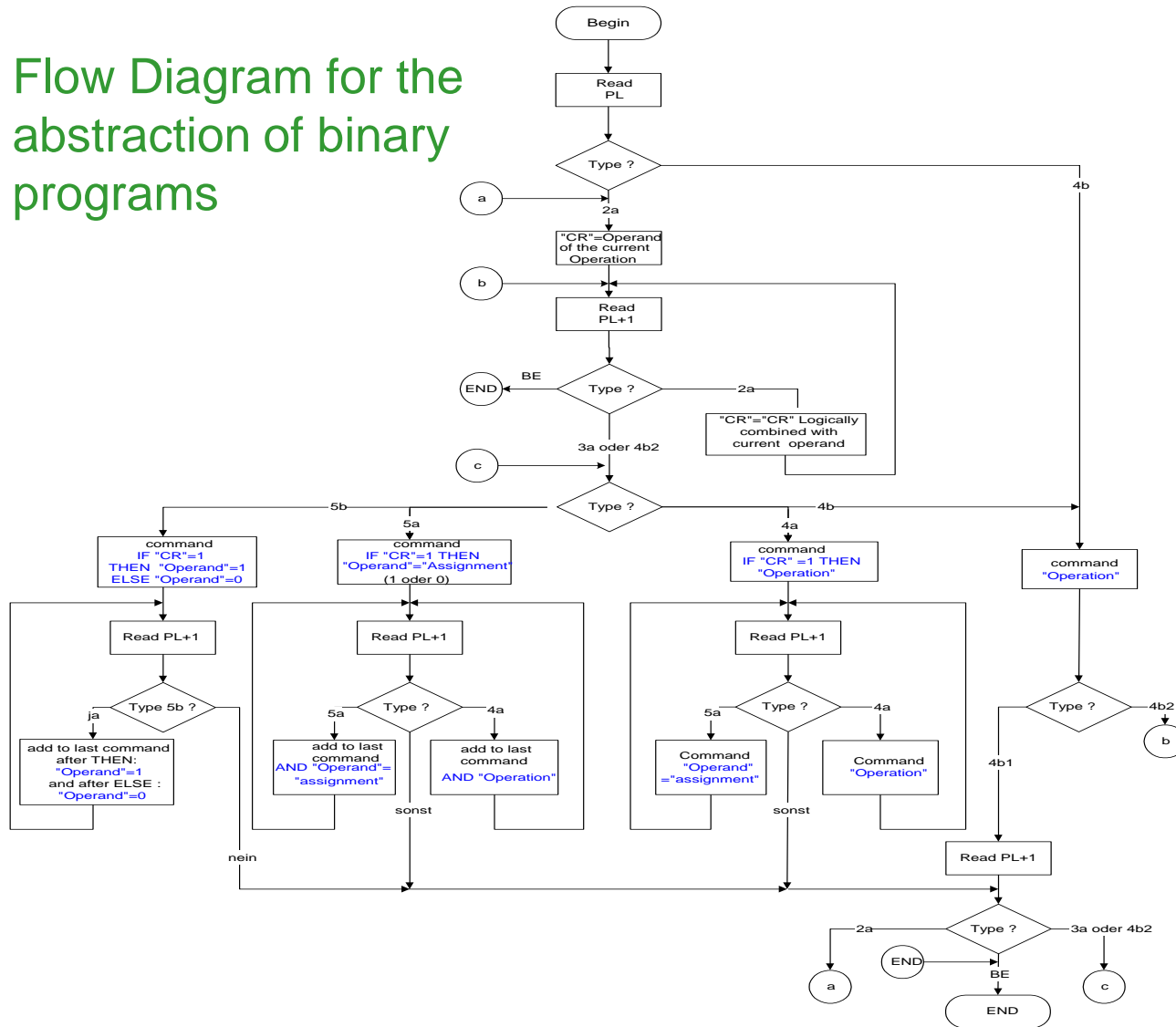
0000      :U      E      38.1
0002      :U      E      18.3
0004      :U      E      20.4
0006      :SPB    LAB1
0008      :U      E      20.6
000A      :S      A      14.1
000B      :SPA    LAB2
000C LAB1  :U      E      20.7
000D      :=      A      15.0
000E LAB2  :O      E      21.0
000F      :=      A      16.0
0010      :BE
    
```

Transformation	No. of states	No. of Transitions	State Contents
Alternative no. 1 (Single Operations)	28 states	29	CR, PC, Variables, output
Alternative no. 2 (University of Cachan)	14 states	13	CR, PC, Variables, output
Alternative no. 3 (Optimization of Alt. 2)	9 states	8	CR, PC, Variables, output
Alternative no. 4 (Abstraction)	6 states	9	PC, Variables
Alternative no. 5 (Moore)	9 states	14	CR, PC, Variables output
Alternative no. 6 (Alt. 4 no contents)	6 states	9	No State contents

Comparison of the transformations

Typ 1			Typ 2		Typ 3		Typ 4			Typ 5	
1a	1b	1c	2a	2b	3a	3b	4a	4b		5a	5b
								4b1	4b2		
S R SPB BAB BEB	SI SV SE SA ZV ZR	SA	U UN O ON O U(O()	SPB BAB BEB	S R = SI SV SE SS SA ZV ZR SPA BA SPB BAB BE BEB BEA	O U(O()	SPB BAB BEB	SPA BA BE BEA	A,A X E,EX	S R	=

Flow Diagram for the abstraction of binary programs



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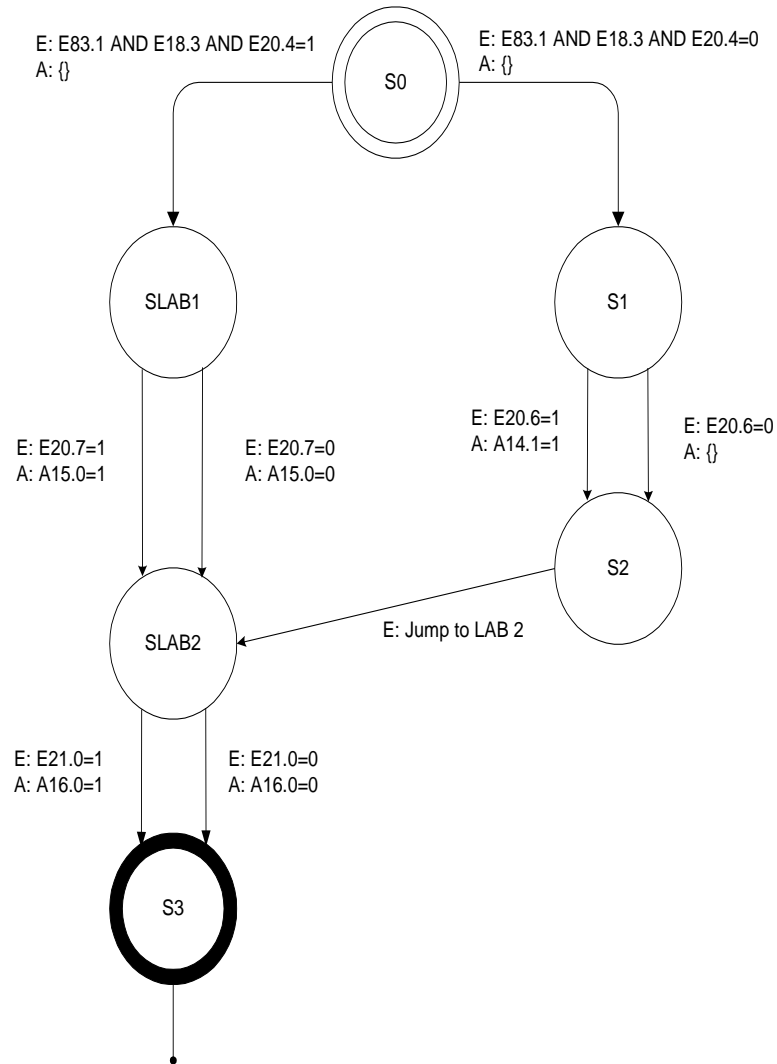
Case Stud.

Summary

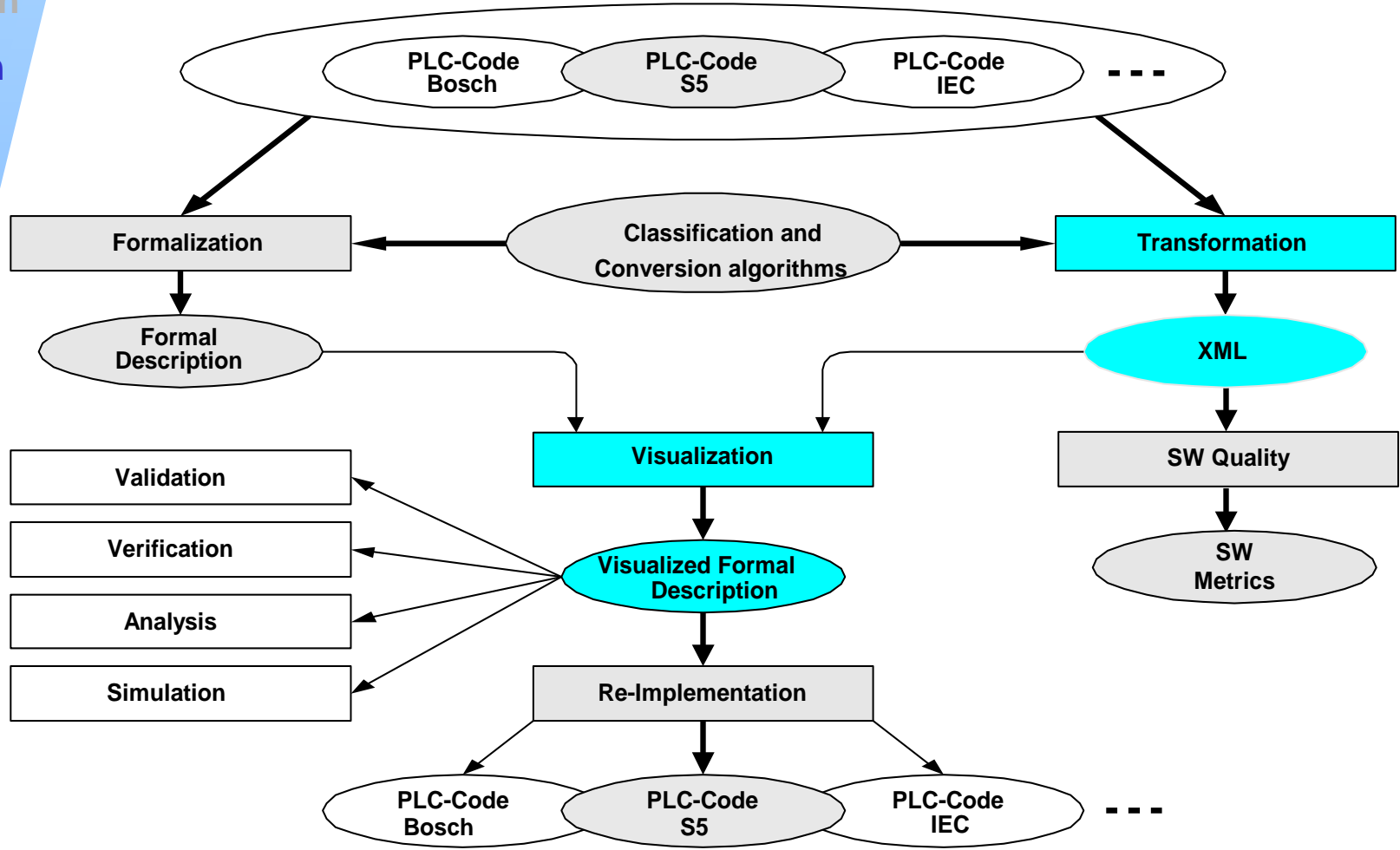
0000		:U	E	38.1
0002		:U	E	18.3
0004		:U	E	20.4
0006		:SPB	LAB1	
0008		:U	E	20.6
000A		:S	A	14.1
000B		:SPA	LAB2	
000C	LAB1	:U	E	20.7
000D		: =	A	15.0
000E	LAB2	:O	E	21.0
000F		: =	A	16.0
0010		:BE		

```

IF U E 38.1 U E 18.3 U E 20.4 = 1
THEN Jump to LAB1
IF U E 20.6 = 1
THEN A 14.1=1
Jump to LAB2
LAB1 IF U E 20.7 = 1
THEN A 15.0=1
ELSE A 15.0=0
LAB2 IF O E 21.0 = 1
THEN A 16.0=1
ELSE A 16.0=0
BE
  
```



- Visualization concept in a compound re-eng.
- Use of XML as an intermediate step



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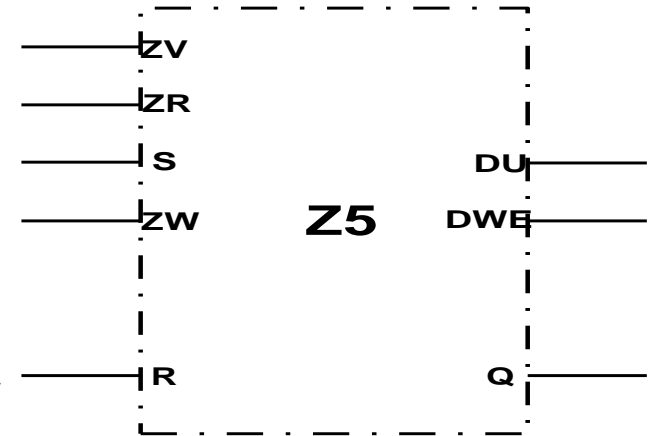
SW-Quality

Case Stud.

Summary

Outlook

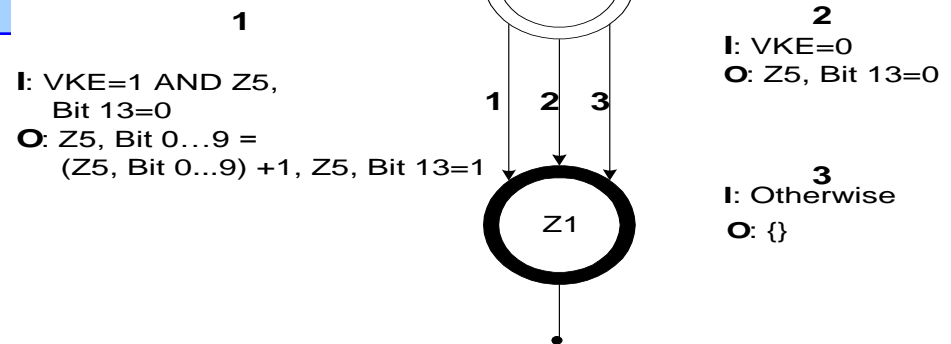
- Need for counters and counters
- Counting range 000 up to 999
- 16 bit word for a counter word consists of:
 - State bits → to process the counter
 - Counting Value → real value of the counter
- Set a counter:



Function block of a counter (Z5)

```

ZV Z5  IF    „VKE“=1 AND Z5, Bit13=0
      THEN  Z5, Bit0...9=(Z5, Bit0...9)+1
           AND Z5, Bit13=1
      ELSE  IF    „VKE“=0
      THEN  Z5, Bit 13=0
    
```



Need to ask for the state for the Counter using U Z5

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Outlook

- Non-Binary Programs extends Binary to allow other types of controls Data Handling, Numerical Logic, and Lists.
- Abstraction of digital operations to IF-THEN- ELSE Algorithms

Types of Non-Binary Operations

Type	Operations
1	Load operation
2	Transfer operation
3	Arithmetic operation
4	Compare operation
5	Digital logical operation
6	1s complement operation
7	2s complement operation
8	Shift and rotate operation
9	Jump operation
10	Other operation

- Transformation of IF-THEN- ELSE Algorithms into Mealy FSM
- Optimization of the Abstraction according to optimization algorithm

Example

PLC Code

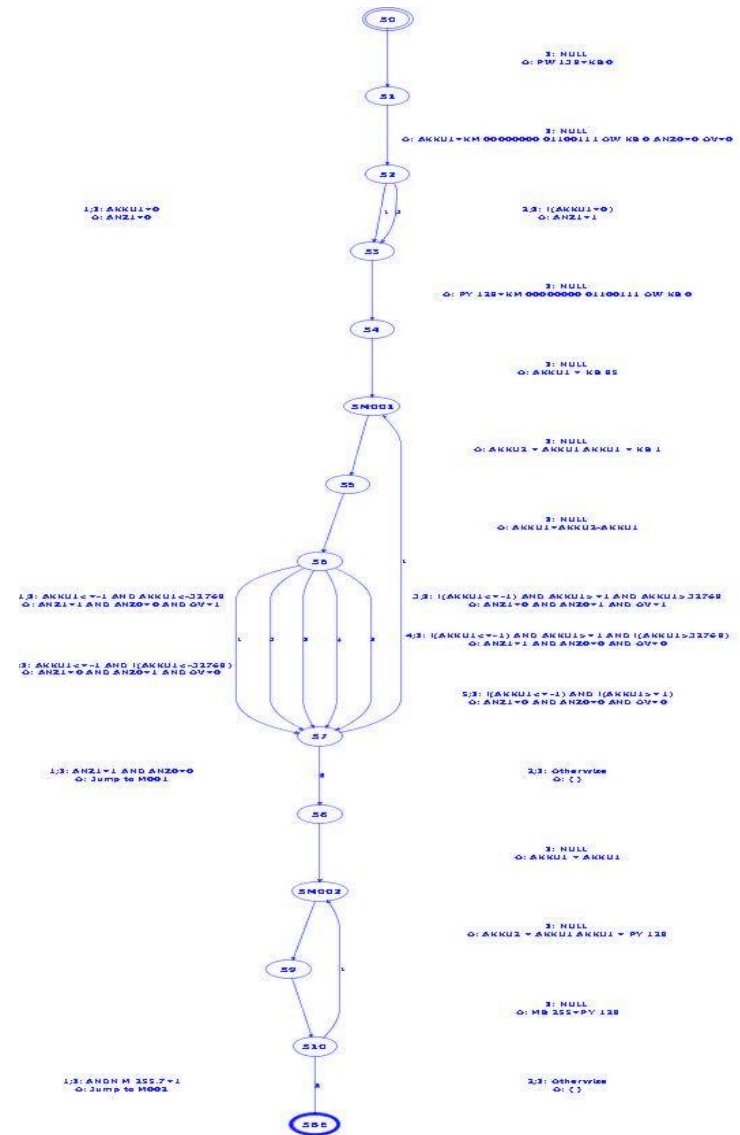
```

0001      :L      KB0
0002      :T      PW138
0003      :L      KM0000000010011
0004      :OW
0005      :T      PY128
0006      :L      KB85
0007 M0    :L      KB1
0008      :-F
0009      :SPZ=   M0
000A M2    :L      PY28
000B      :T      MB225
000C      :UN     M225.7
000D      :SPB=   M2
000E      :BE
    
```

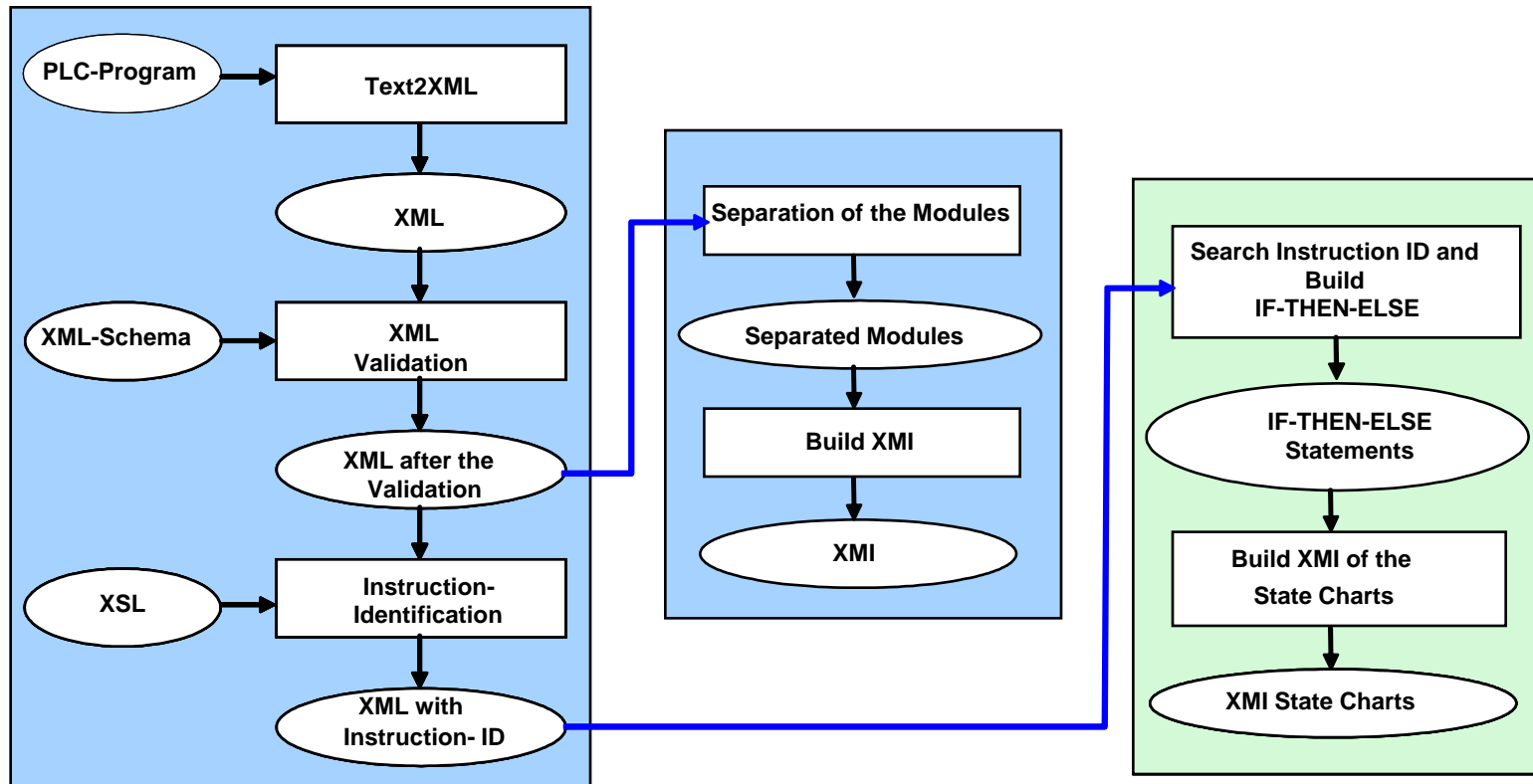
IF_THEN_ELSE

```

PW138 = KB0
AKKU 1 = KM0000000010011OW KB0
ANZ0 = 0 AND OV = 0
IF AKKU 1 = 0 THEN ANZ1 = 0 ELSE ANZ1 = 1
PY128 = AKKU 1
AKKU 1 = KB 85
M0      AKKU 2 = AKKU 1
        AKKU 1 = KB1
        AKKU1 = AKKU 2-AKKU 1
        IF AKKU1 <= -1
        THEN  IF AKKU1 < -32768
                THEN ANZ1 = 1 AND ANZ0 = 0 AND OV = 1
                ELSE ANZ1 = 0 AND ANZ0 = 1 AND OV = 0
        ELSE  IF AKKU1 >= 1
                THEN  IF AKKU1 > 32768
                        THEN ANZ1 = 0 AND ANZ0 = 1 AND OV = 1
                        ELSE ANZ1 = 1 AND ANZ0 = 0 AND OV = 0
                ELSE ANZ1 = 0 AND ANZ0 = 0 AND OV = 0
        IF ANZ1 = 0 AND ANZ0 = 0 THEN Jump to M0
M2      MB225 = PY28
        IF (N M225.7) = 1 THEN Jump To M2
        BE
    
```



Steps toward the conversion



→ State Charts as a visualization alternative

COM CGI JavaScript C# XHTML Java OS SMTP WML
 IP FTP JNI DOM
 XSL XML RTF XPath DNS HTTP
 Email SOAP XLink eCl@ss B2B TCP RMI eCommerce Corba
 HTML DTD NNTP Perl WWW SAX JVM News Java

programming
languages

services

protocols

models

interfaces



mark-up
languages

operating
systems

schemes

Fields of Application

- eCommerce
- asset management
- remote engineering
- remote control
- remote maintenance

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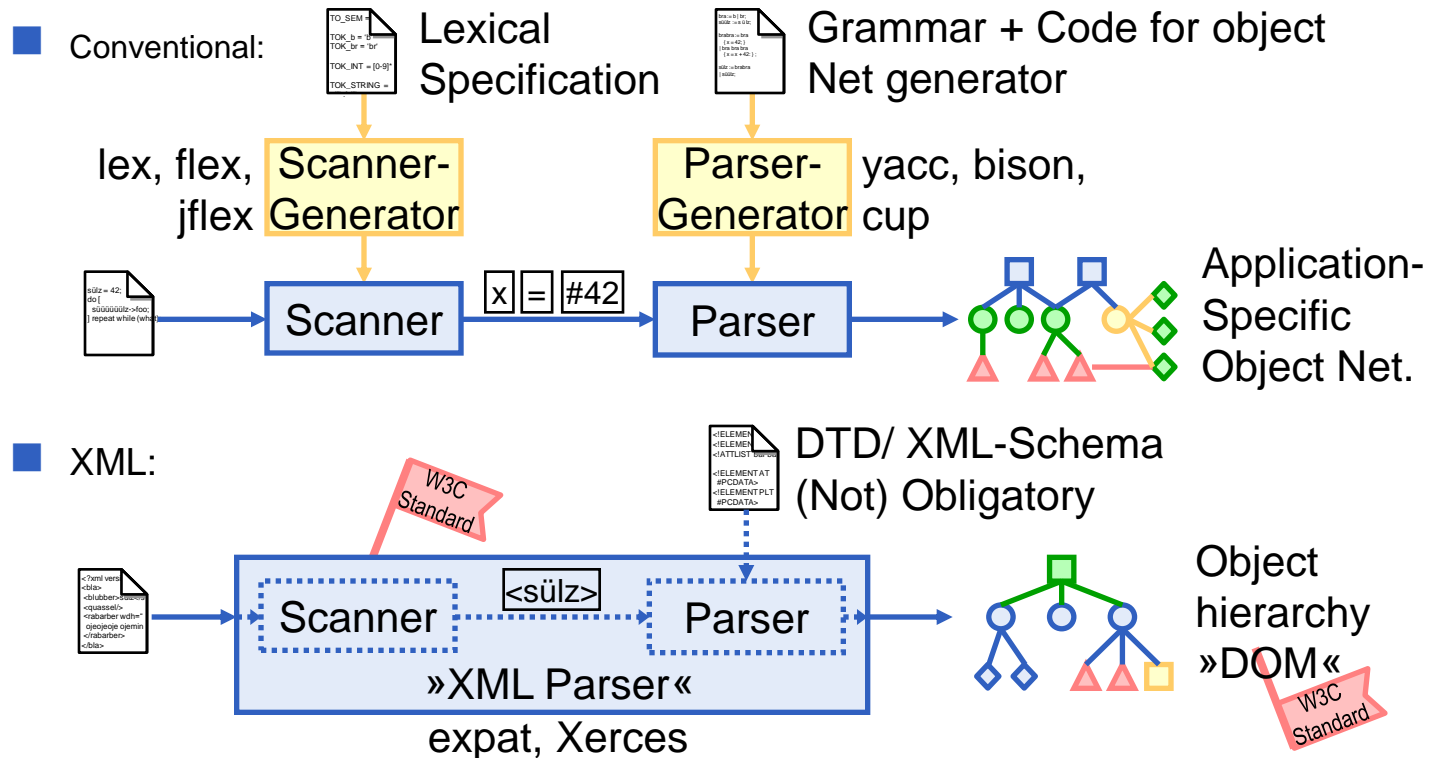
SW-Quality

Case Stud.

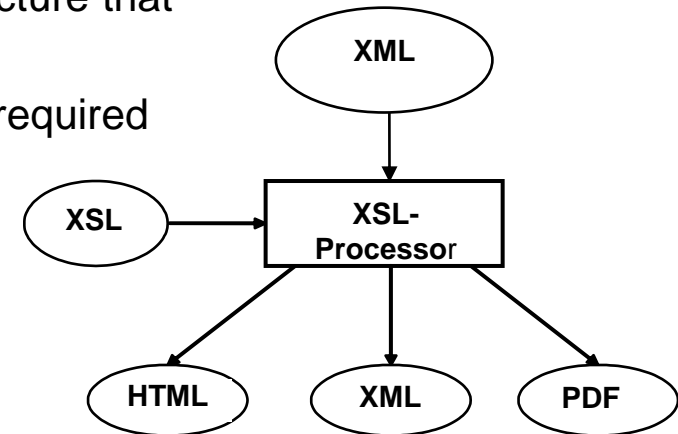
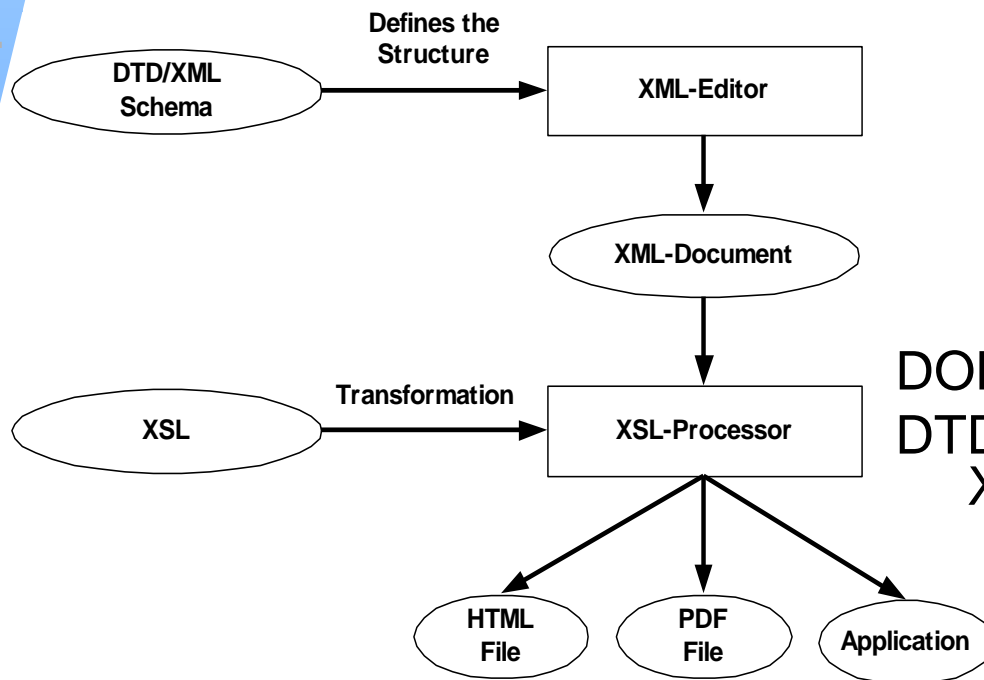
Summary

Outlook

- XML (eXtensible Markup Language)
- XML and HTML
- XML to exchange information across platforms and applications.
- How to apply XML?

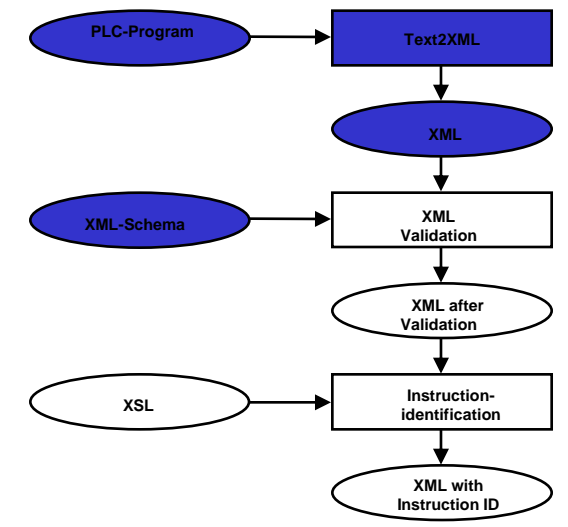
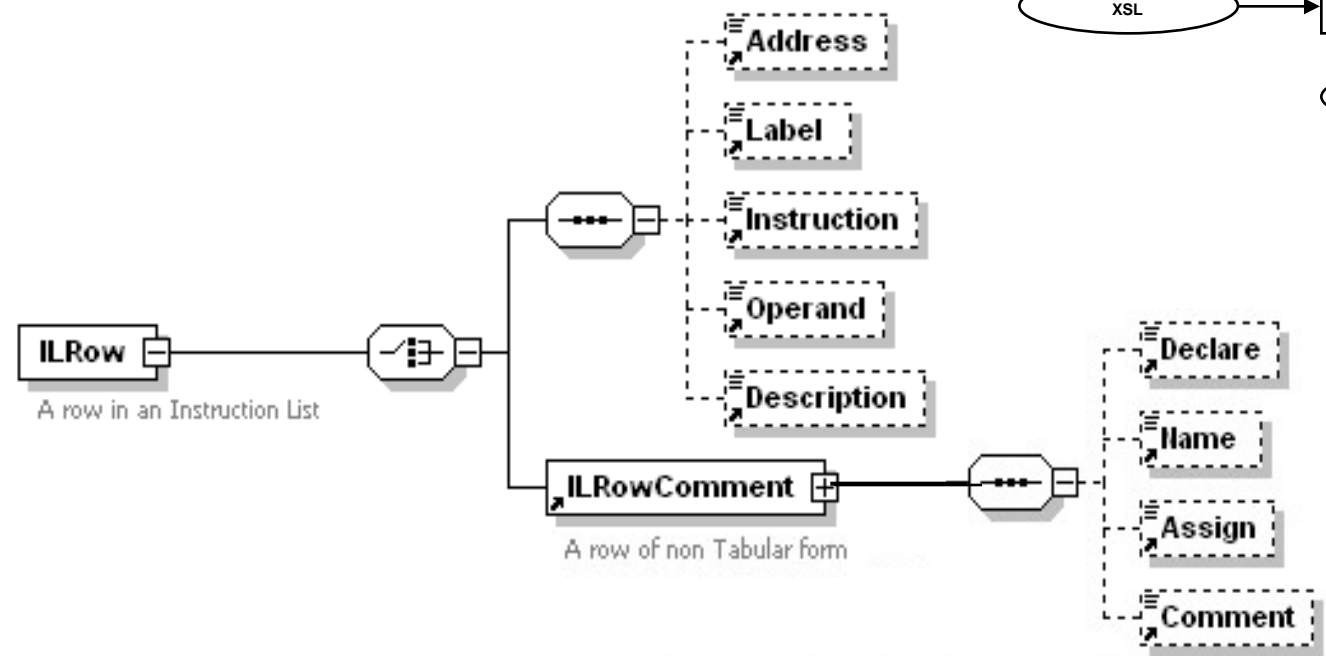
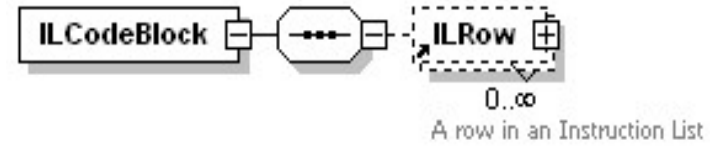


- XSL (stylesheet language for XML) and XSLT (XSL transformation)
- XSLT functions in two steps
 - structural transformation XML → structure that reflects the desired output
 - formatting the new structure into the required format, such as HTML or PDF



DOM (Document Object Model)
DTD (Document Type Definition) or
XML-Schema

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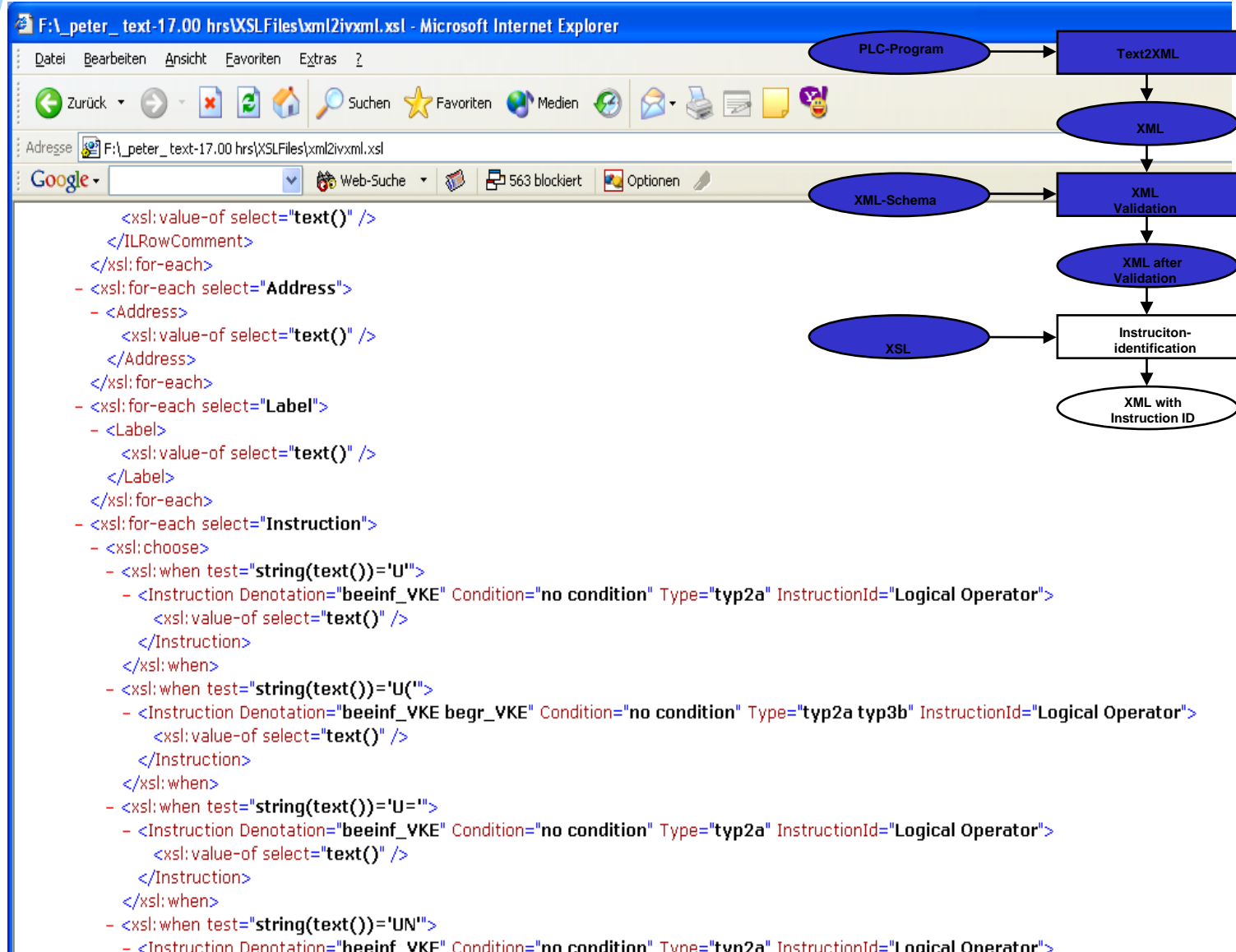
Re-Implem.

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Outlook



The screenshot shows a web browser displaying XSL code. The code uses `<xsl:for-each>` loops to iterate over `Address`, `Label`, and `Instruction` elements. The `Instruction` loop uses `<xsl:choose>` and `<xsl:when>` to identify specific instructions like `beeinf_VKE` and assign them an `InstructionId`.

On the right side, a flowchart illustrates the process:

- PLC-Program** (oval) feeds into **Text2XML** (rectangle).
- Text2XML** outputs **XML** (oval).
- XML** feeds into **XML Validation** (rectangle).
- XML Validation** outputs **XML after Validation** (oval).
- XML after Validation** feeds into **Instrucion-identification** (rectangle).
- XSL** (oval) also feeds into **Instrucion-identification**.
- Instrucion-identification** outputs **XML with Instruction ID** (oval).

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OB 1

NETZWERK 1

0000 :SPA PB 1 Jump Absolute to PE

0002 :BE

PB 1

NETZWERK 1

```

0000:U   E38.1      //AND Operation
0002:U   E38.2
0004:O
0006:U   E38.1      //OR Operation
0008:U   E38.3
000A     :O
000C     :U         E38.2
000E     :U         E38.3
0010:=   M100.0    at least two Fans running
0012:UN  E38.1      // ANDN Operation
0014:UN  E38.2
0016:UN  E38.3
0018:=   M100.1    no running Fan
001A     :U(
001C     :O         M100.0 Continuous Light
001E     :O
0020:U   M100.1
0022:U   M99.1     Flashing with 2 Hz
0024:O
0026:UN  M100.0
0028:UN  M100.1
002A     :U         M99.2 Flashing with 0,5 Hz
002C     :)
002E     :U         A42.4 „Active“
0030:=   A51.7     LCD lamp
0032:BE
    
```

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U	Logical Operator
U	Logical Operator
O	Logical Operator
U	Logical Operator
U	Logical Operator
O	Logical Operator
U	Logical Operator
U	Logical Operator
=	Assignment
UN	Logical Operator
UN	Logical Operator
UN	Logical Operator
=	Assignment
U(Logical Operator
O	Logical Operator
O	Logical Operator
U	Logical Operator
BE	Special Operation

UML - OMG's Unified Modeling Language - is a graphical language that expresses application requirements analysis and program design in a standard way. Methodology-independent, UML is used by dozens of analysis and design (A&D) tools on the market, making it OMG's most widely used specification.

UML standardizes four types of structural diagrams:

- Class diagram
- Object diagram
- Component diagram
- Deployment diagram

also five types of behavioral diagrams:

- Use Case diagram
- Sequence diagram
- Collaboration diagram
- Statechart diagram
- Activity diagram

and three types of model management diagrams:

- Package diagram
- Model diagram
- Subsystem diagram

Standardization allows design tools to interchange models using XMI

XMI, XML-eXtensible Markup Language, a W3C standard

is an international industry-standard defined by the Object Management Group OMG

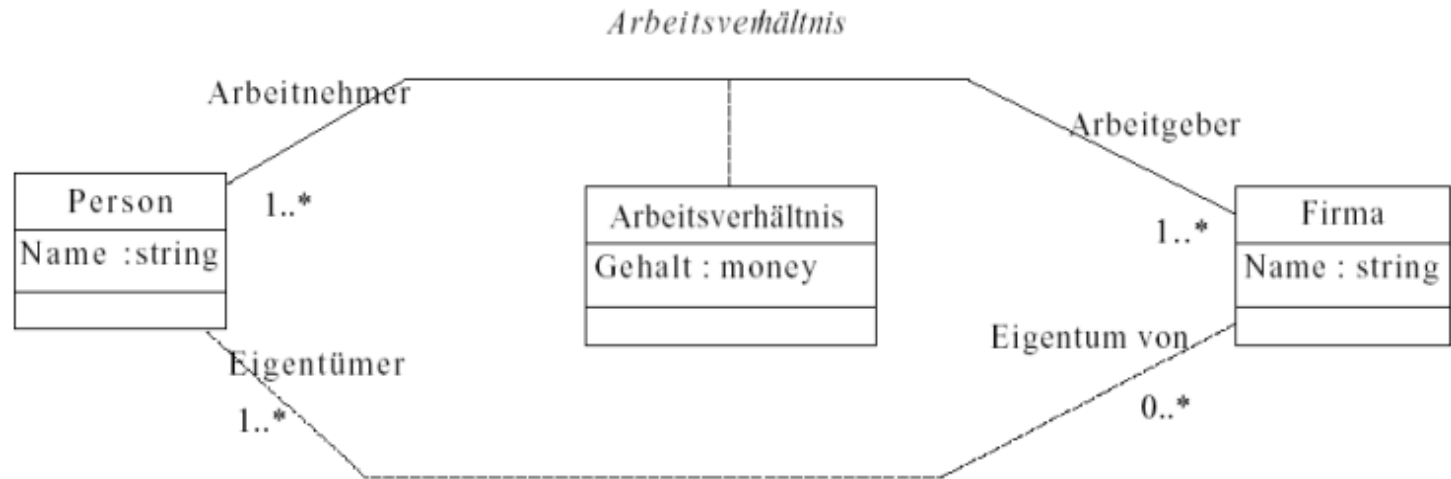
is a stream format for interchange of metadata including the UML models that you create during your analysis and design activities

It's useful for transferring the model from one step to the next as your design and coding progress

or for transferring from one design tool to another.

because XMI streams models into XML datasets, it also serves as a mapping from UML to XML

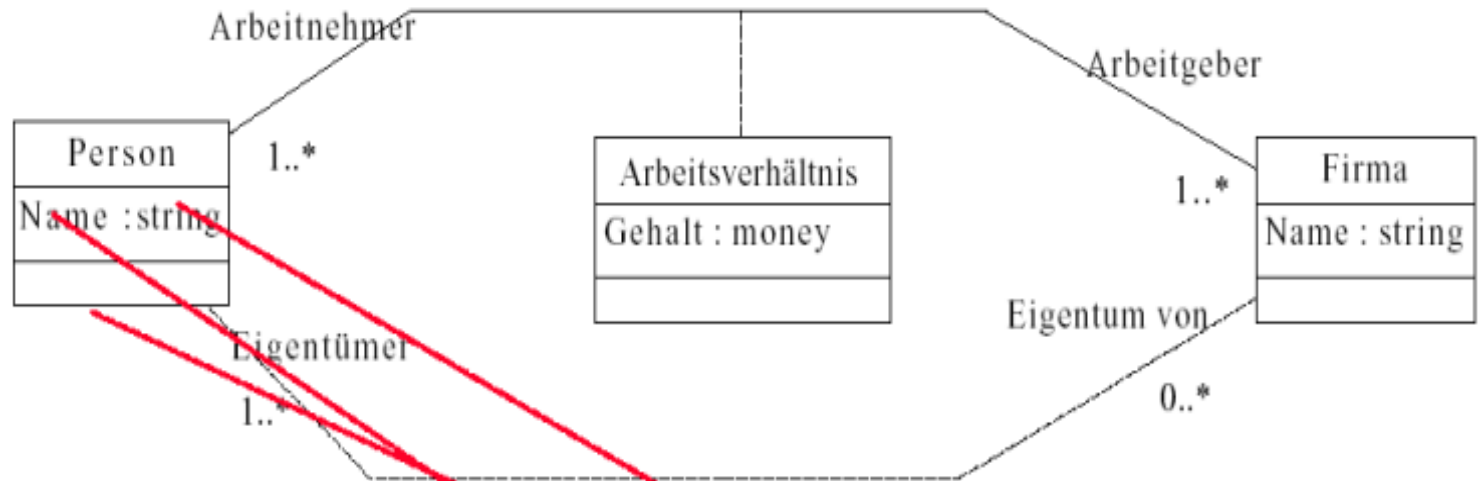
SW tools available made it possible to integrate XMI to UML (by import project from XMI or export project to XMI)



```

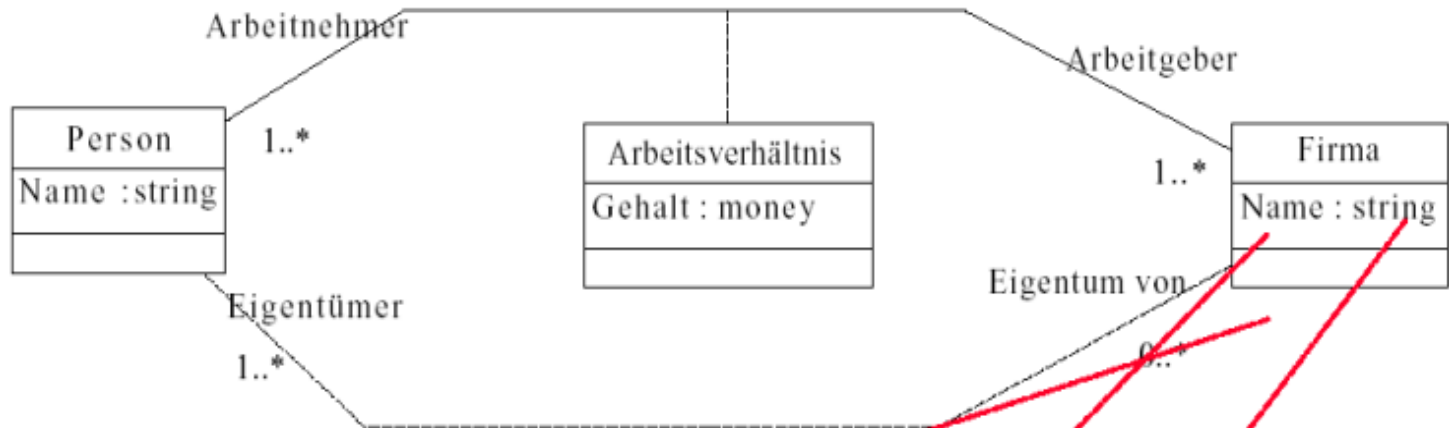
<XMI timestamp="2000-10-09T17:00:00" verified="true" xmi.version="1.1">
  <XMI.header>
    <XMI.model xmi.name="SimpleClassModel"/>
    <XMI.metamodel xmi.name="UML" xmi.version="1.3"/>
  </XMI.header>

```



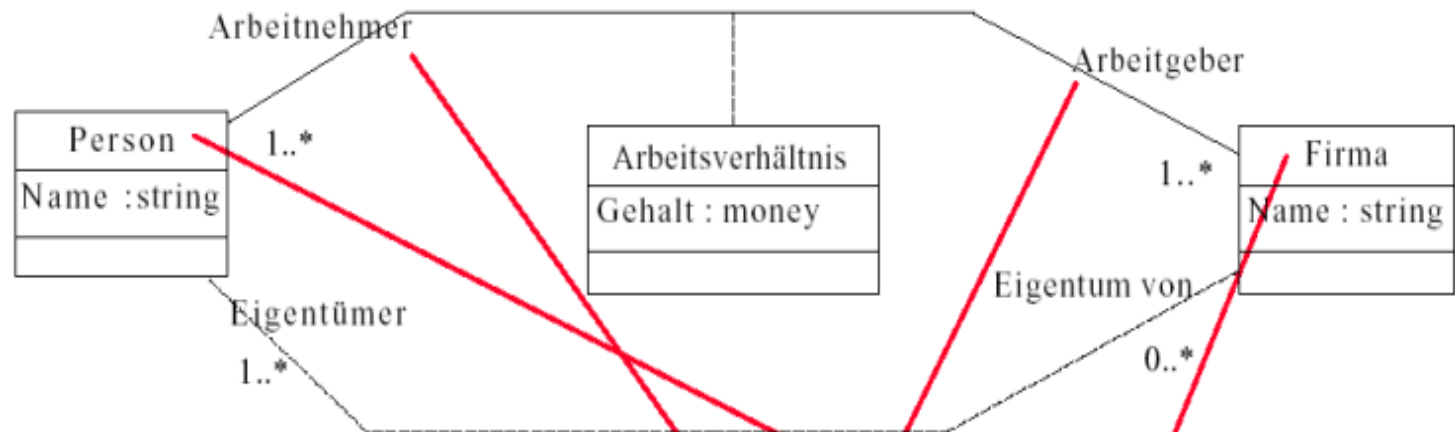
```

<XMI.content>
  <UML:Class name="Person" xmi.id="Person">
    <UML:Classifier.feature>
      <UML:Attribute name="Name" type="string"/>
    </UML:Classifier.feature>
  </UML:Class>
  
```



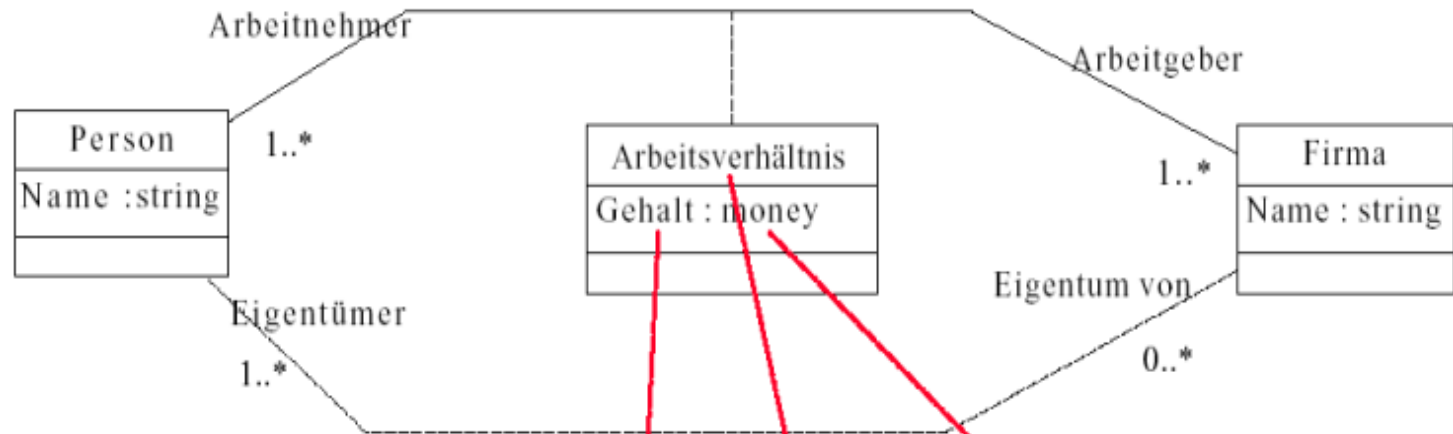
```

<UML:Class name="Firma" xmi.id="Firma">
  <UML:Classifier.feature>
    <UML:Attribute name="Name" type="string" />
  </UML:Classifier.feature>
</UML:Class>
  
```

```

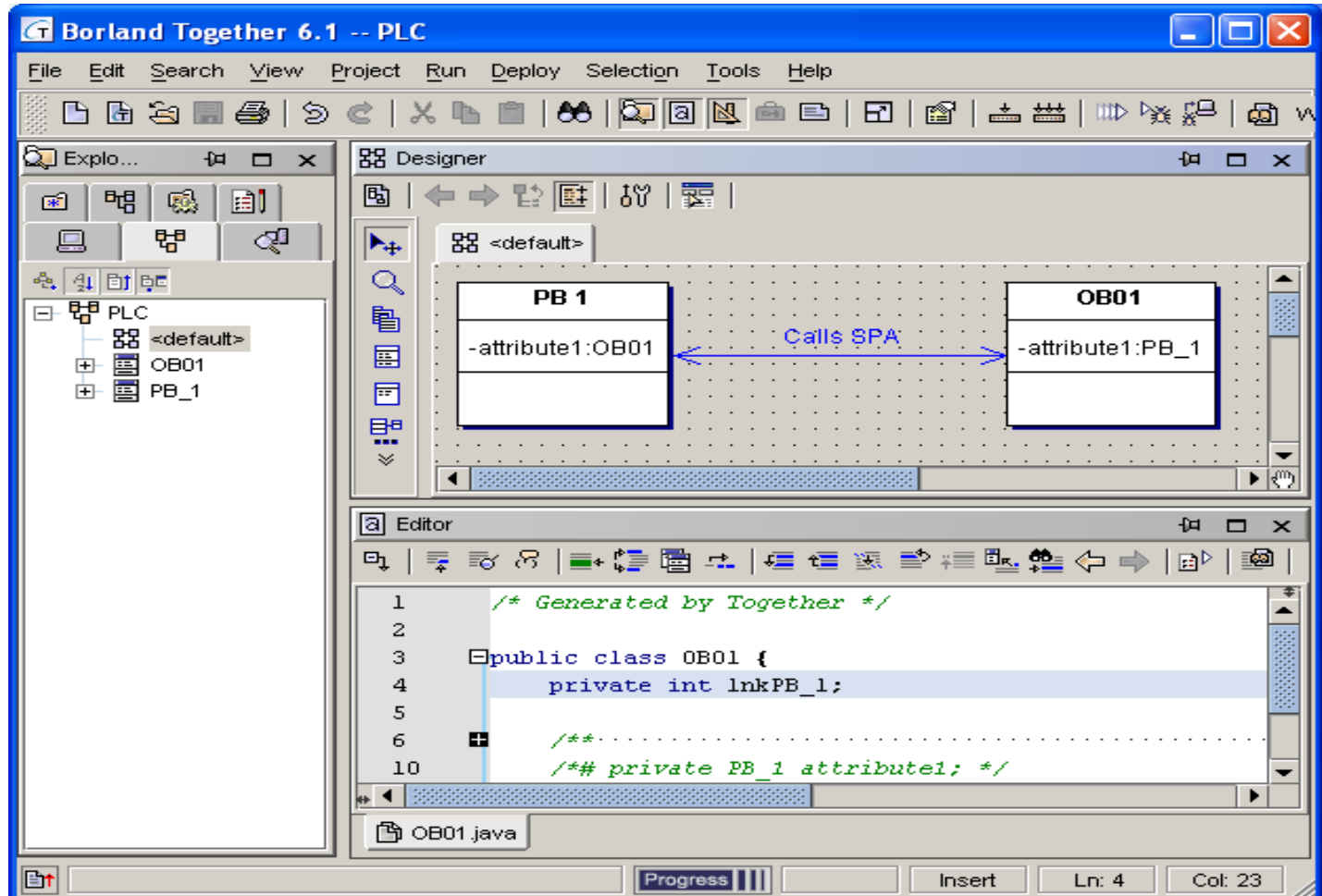
<UML:Association>
  <UML:Association.connection>
    <UML:AssociationEnd name="Arbeitnehmer" type="Person"/>
    <UML:AssociationEnd name="Arbeitgeber" type="Firma"/>
  </UML:Association.connection>
</UML:Association>
  
```



```

<UML:AssociationClass name="Arbeitsverhältnis">
  <UML:Classifier.feature>
    <UML:Attribute name="Gehalt" multiplicity="1..1" type="money"/>
  </UML:Classifier.feature>
</UML:AssociationClass>
  
```

UML of OB 1 imported in Together



The screenshot shows the Borland Together 6.1 -- PLC interface. The main window is divided into several panes:

- Explorer:** Shows a project tree with a folder named "PLC" containing sub-elements "<default>", "OB01", and "PB_1".
- Designer:** Displays a UML class diagram with two classes: "PB 1" and "OB01". "PB 1" has an attribute "-attribute1:OB01" and "OB01" has an attribute "-attribute1:PB_1". A bidirectional association arrow labeled "Calls SPA" connects the two classes.
- Editor:** Shows the source code for "OB01.java":


```

1      /* Generated by Together */
2
3      public class OB01 {
4          private int lnkPB_1;
5
6          /** .....
10         /**# private PB_1 attributel; */
      
```

The status bar at the bottom indicates "Progress", "Insert", "Ln: 4", and "Col: 23".

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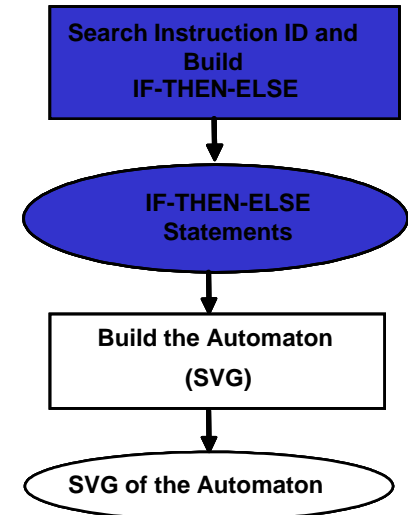
SW-Quality

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Summary

Outlook

PB 1		
NETZWERK	1	
0000:U	E38.1	//AND Operation
0002:U	E38.2	
0004:O		//OR Operation
0006:U	E38.1	
0008:U	E38.3	
000A	:O	
000C	:U	E38.2
000E	:U	E38.3
0010:=	M100.0	at least two Fans running
0012:UN	E38.1	// ANDN Operation
0014:UN	E38.2	
0016:UN	E38.3	
0018:=	M1	
001A	:U(
001C	:O	
001E	:O	
0020:U	M1	
0022:U	M9	
0024:O		
0026:UN	M1	
0028:UN	M1	
002A	:U	
002C	:)	
002E	:U	
0030:=	A5	
0032:BE		



001A	:U(IF	(E 38.1 AND E 38.2) OR (E 38.1 AND E 38.3) OR (E 38.2
001C	:O		AND E 38.3) =1
001E	:O	THEN	M 100.0=1
0020:U	M1	ELSE	M 100.0=0
0022:U	M9	IF	NOT E 38.1 ANDN E 38.2 ANDN E 38.3 =1
0024:O		THEN	M 100.1=1
0026:UN	M1	ELSE	M 100.1=0
0028:UN	M1	IF	(M 100.0) OR (M 100.1 AND M 99.1) OR (NOT M 100.0
002A	:U		ANDN M 100.1 AND M 99.2) AND A 42.4 =1
002E	:U	THEN	A 51.7 =1
0030:=	A5	ELSE	A 51.7=0
0032:BE		BE	

```

IF          (E 38.1 AND E 38.2) OR
              (E 38.1 AND E 38.3) OR
              (E 38.2 AND E 38.3) =1
THEN       M 100.0=1
ELSE       M 100.0=0
IF          NOT E 38.1 ANDN E 38.2
              ANDN E 38.3 =1
THEN       M 100.1=1
ELSE       M 100.1=0
IF          (M 100.0) OR (M 100.1 AND
              M 99.1) OR (NOT M 100.0
              ANDN M 100.1 AND M 99.2)
              AND A 42.4 =1
THEN       A 51.7 =1
ELSE       A 51.7=0
BE
    
```

```

<?xml version="1.0" encoding="UTF-8" ?>
<fsm name="PB001">
  <state name="Si">
    <transition action="NULL" input="?Call PB001" next="S0" />
  </state>
  <state name="S0">
    <transition action="M 100.0=1" input="E38.1 AND E38.2 OR
    E38.1 AND E38.3 OR E38.2 AND E38.3" next="S1" />
    <transition action="M 100.0=0" input="~ ( E38.1 AND E38.2
    OR E38.1 AND E38.3 OR E38.2 AND E38.3 )" next="S1" />
  </state>
  <state name="S1">
    <transition action="M 100.1=1" input="~ E38.1 ANDN E38.2
    ANDN E38.3" next="S2" />
    <transition action="M 100.1=0" input="~ ( ~ E38.1 ANDN
    E38.2 ANDN E38.3 )" next="S2" />
  </state>
  <state name="S2">
    <transition action="A 51.7=1" input="( M100.0 OR M100.1
    AND M99.1 OR ~ M100.0 ANDN M100.1 AND M99.2 )
    AND A42.4" next="SBE" />
    <transition action="A 51.7=0" input="~ ( ( M100.0 OR
    M100.1 AND M99.1 OR ~ M100.0 ANDN M100.1 AND
    M99.2 ) AND A42.4 )" next="SBE" />
  </state>
  <state name="SBE">
    <transition action="!Ret PB001" input="NULL" next="Si" />
  </state>
</fsm>
    
```

IF (E 38.1 AND E 38.2) OR
(E 38.1 AND E 38.3) OR
(E 38.2 AND E 38.3) =1

THEN M 100.0=1

ELSE M 100.0=0

IF NOT E 38.1 ANDN E 38.2
ANDN E 38.3 =1

THEN M 100.1=1

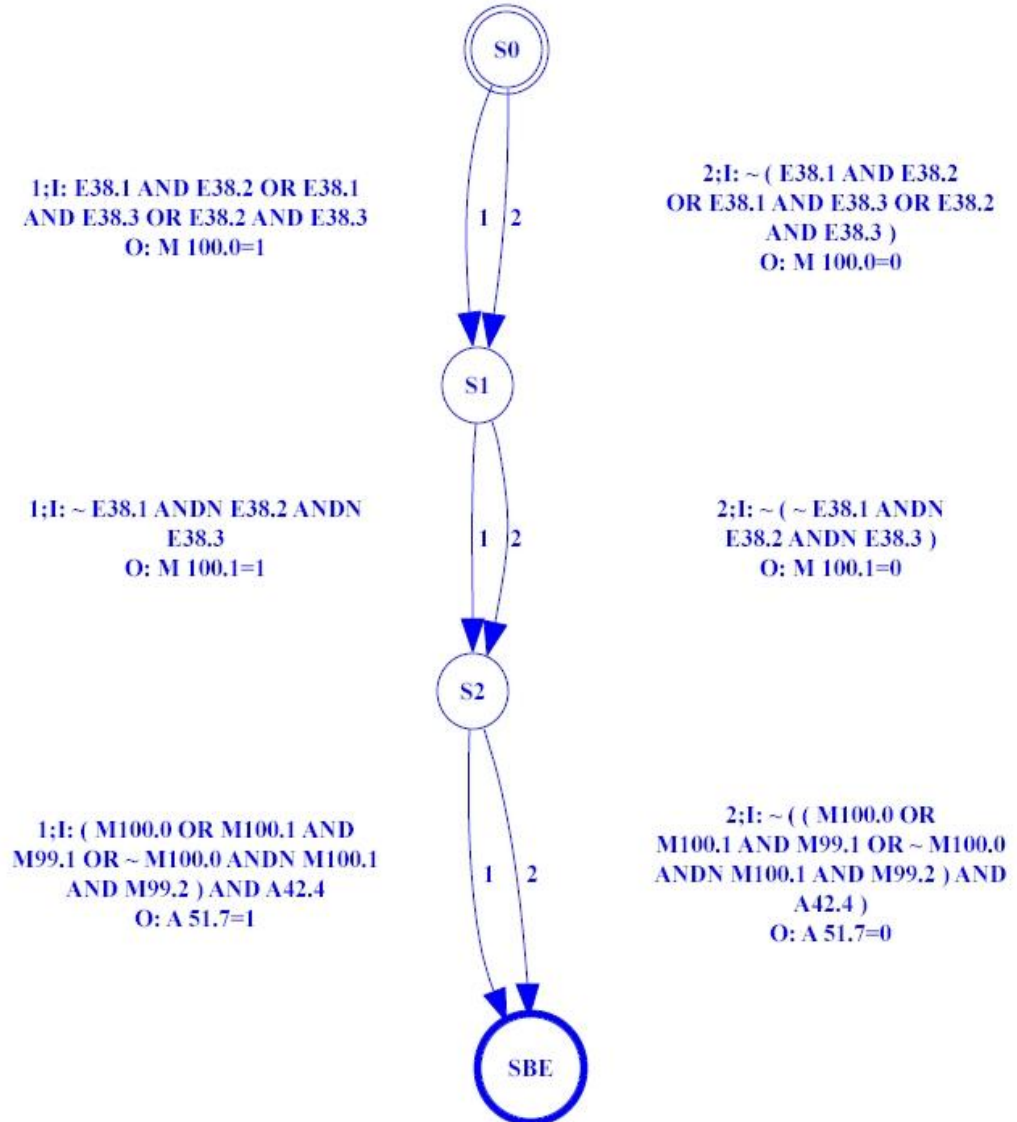
ELSE M 100.1=0

IF (M 100.0) OR (M 100.1 AND
M 99.1) OR (NOT M 100.0
ANDN M 100.1 AND M 99.2)
AND A 42.4 =1

THEN A 51.7 =1

ELSE A 51.7=0

BE



Example: Visualization through SC

IF (E 38.1 AND E 38.2) OR
(E 38.1 AND E 38.3) OR
(E 38.2 AND E 38.3) =1

THEN M 100.0=1

ELSE M 100.0=0

IF NOT E 38.1 ANDN E 38.2
ANDN E 38.3 =1

THEN M 100.1=1

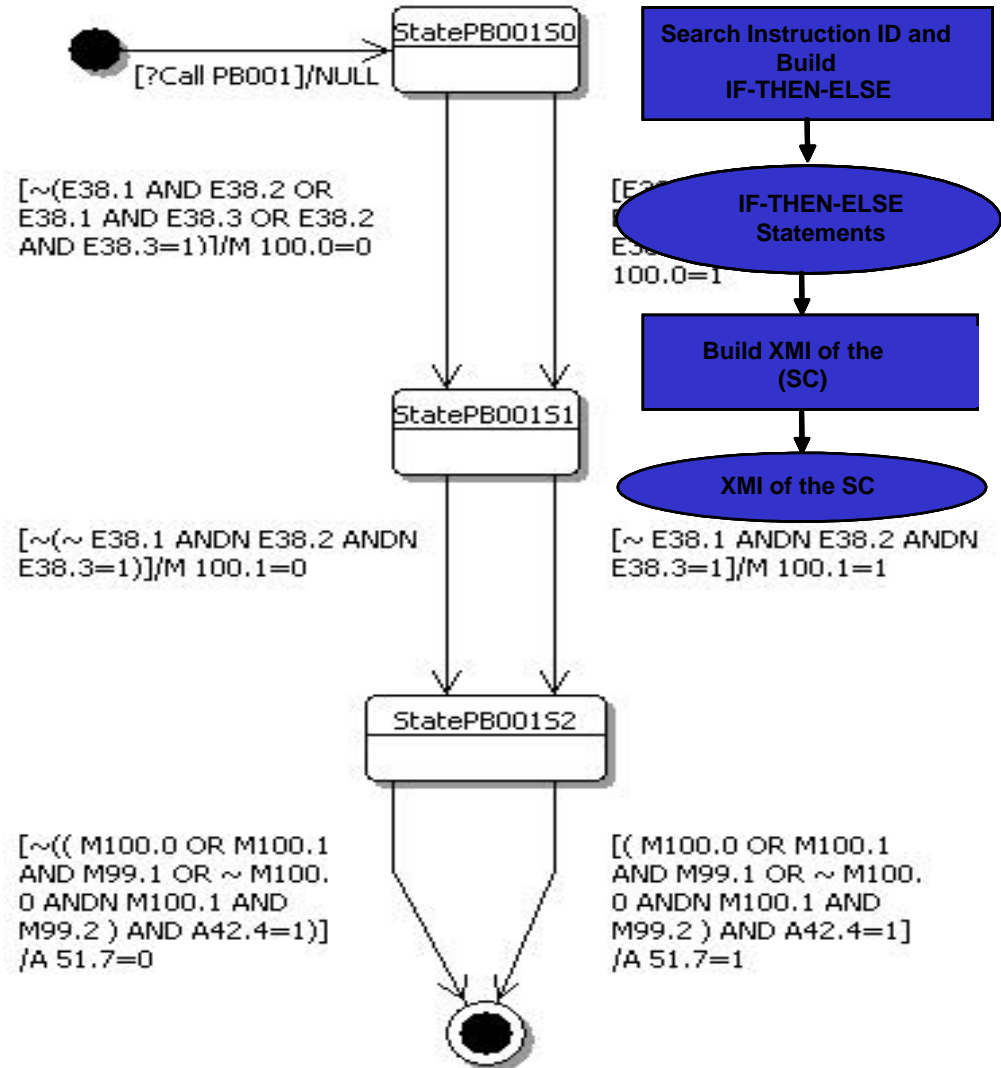
ELSE M 100.1=0

IF (M 100.0) OR (M 100.1 AND
M 99.1) OR (NOT M 100.0
ANDN M 100.1 AND M 99.2)
AND A 42.4 =1

THEN A 51.7 =1

ELSE A 51.7=0

BE



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Outlook

- XML allow the Visualization of the Formalization
- SVG to draw the FSMs
- Extraction of the PLC structure through XMI
- SC as an alternative for the Visualization
- CFSM in XML as a Basis for the Re-Implementation
- XML transformation for deriving the SW-Quality

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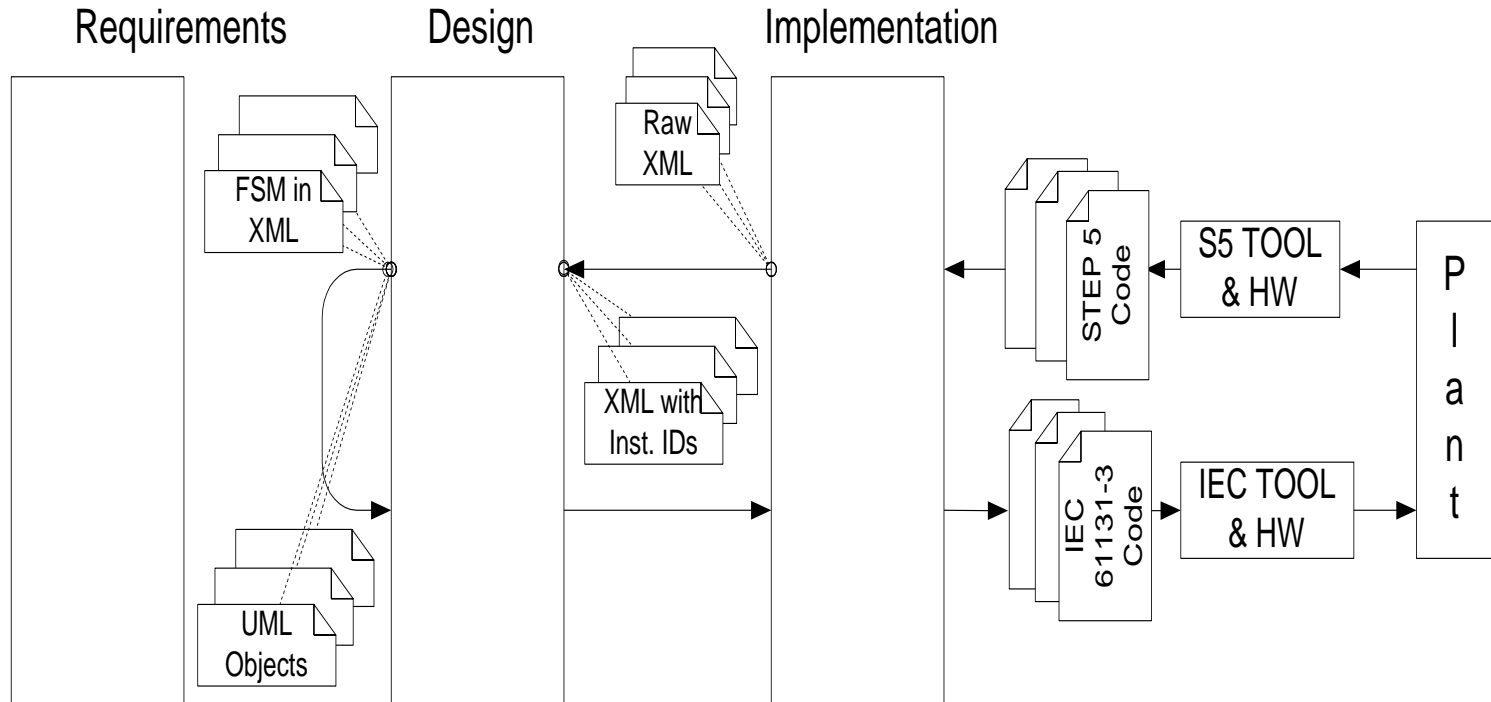
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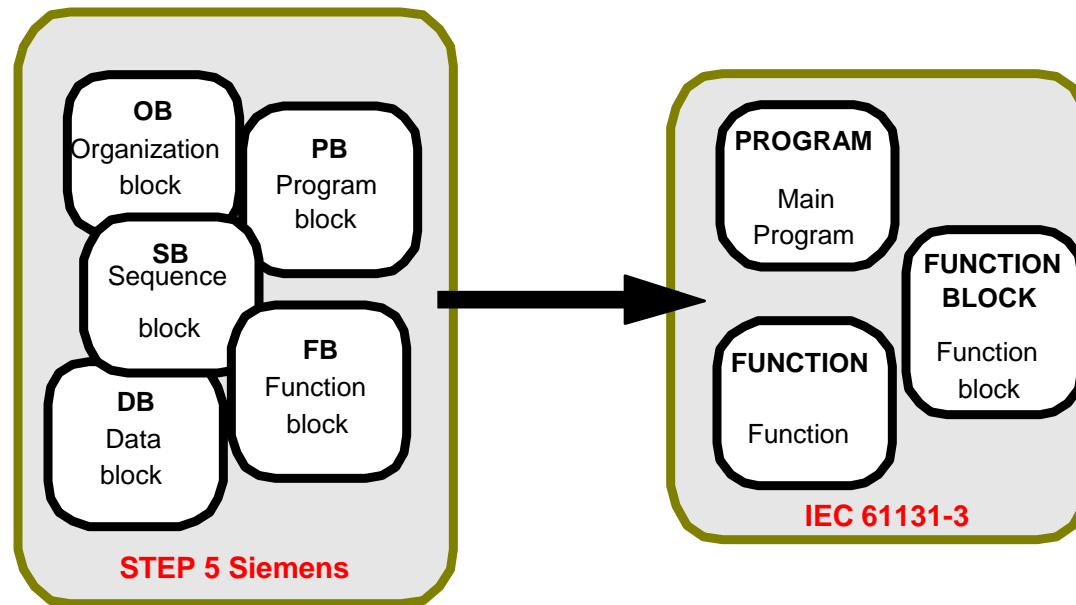
Visualization

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Summary



- OB1 → Program in the new PLC
- PB and FB → Function Blocks
- Other OBs → Programs or Function Blocks
- Data Blocks → Array in IEC 61131-3
- Symbol Table → global addressed variables of the inputs, outputs and internal variables
- Other elements in the STEP 5

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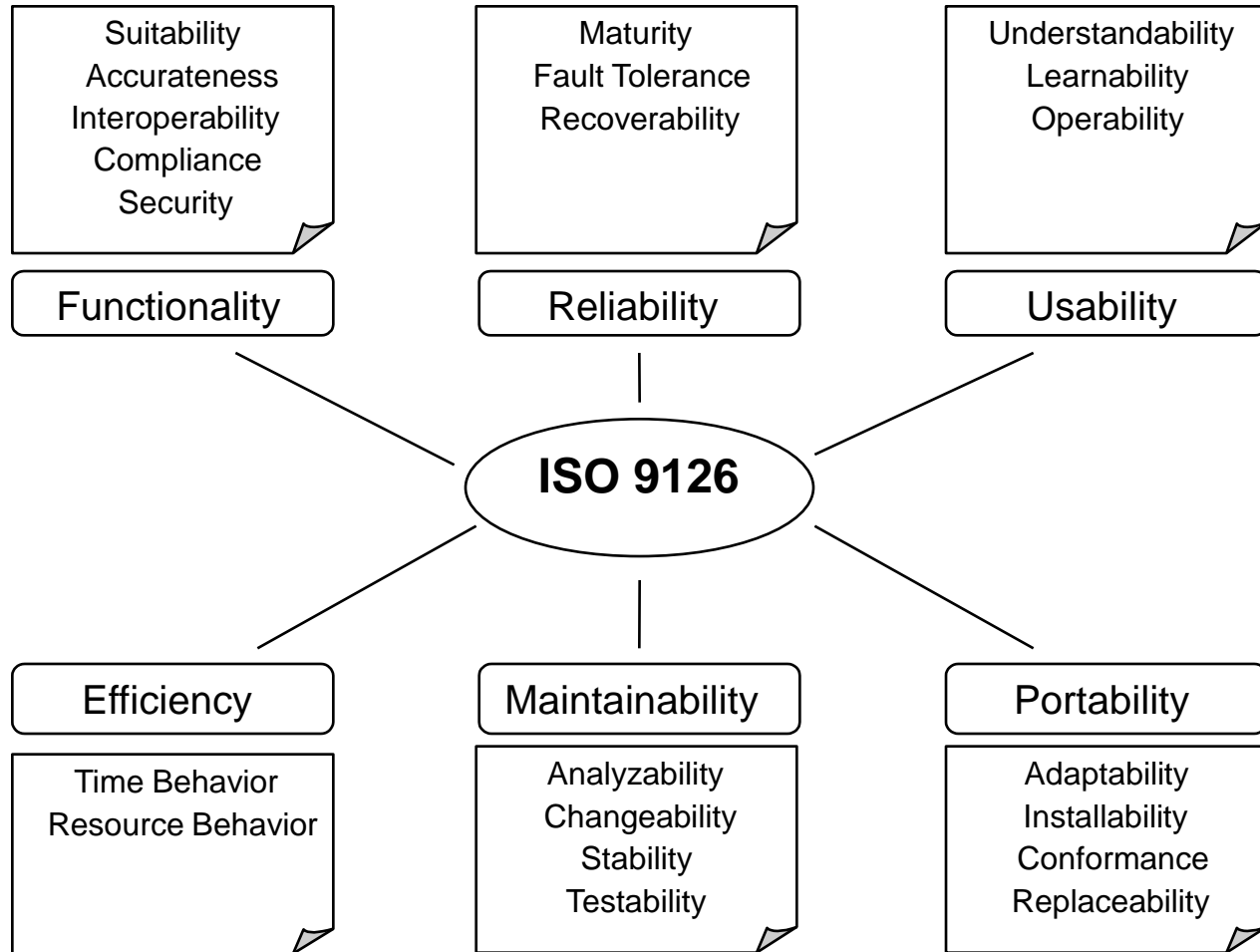
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Criterion	Definition
Functionality	Attributes that bear on the existence of a set of functions and their specified properties. The functions are those that satisfy a stated or implied need.
Reliability	Set of attributes, that bear on the capability of software to maintain its level of performance under stated conditions for a stated period of time.
Usability	Attributes that bear on the effort needed for use, and on the individual evaluation of such use, by a stated or implied set of users.
Efficiency	Attributes that bear on the relationship between the level of the performance of the software and the amount of resources used, under stated conditions
Portability	Attributes that bear on the ability of software to be transformed from one environment to another.
Maintainability	Attributes that bear on the effort needed to make specified modifications

Name	practicability in Software	Usability to IL	Diagnosability Explanatory	Later use for the Diagnosis (online)
Size	++	++	- (Serves for the coarse appraisal)	--
Halstead	++	++	0 (Overview about operators and operands)	--
McCabe Cyclomatic Complexity	+	0 (Graph is necessary)	- (Information about conditioned jumps)	--
Information flow	0	- (flow definition?)	0 (Variables flow bet. Blocks)	0
Tree Impurity	0	+ (Graph is necessary)	+ (Blocks call)	--
Coupling	-	- (interconnection Definition)	0 (Variables flow bet. Blocks)	--

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- Basic Principles for the implemented metrics
 1. Search after assignment instructions (S; R; =)
 2. Record the assignment instruction with its relating Variable
 3. Record all Elements that exist between the current and the last assignment instruction
 4. Setting up the Condition Equation and showing it

U E 12.1

U(

U M 33.1

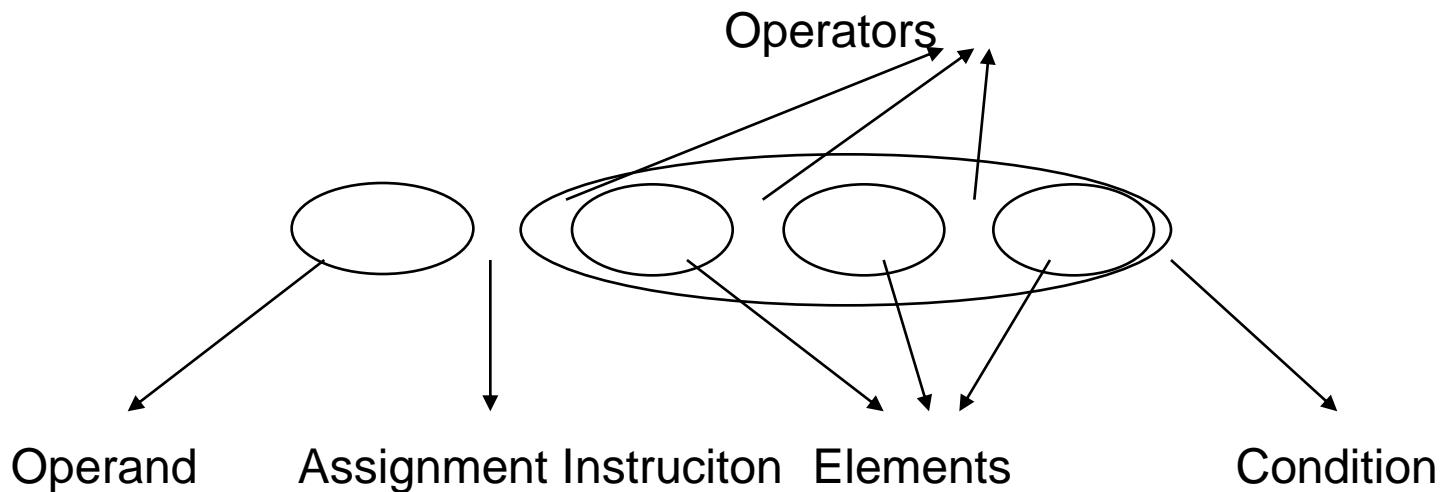
S M 33.3

U M 33.3

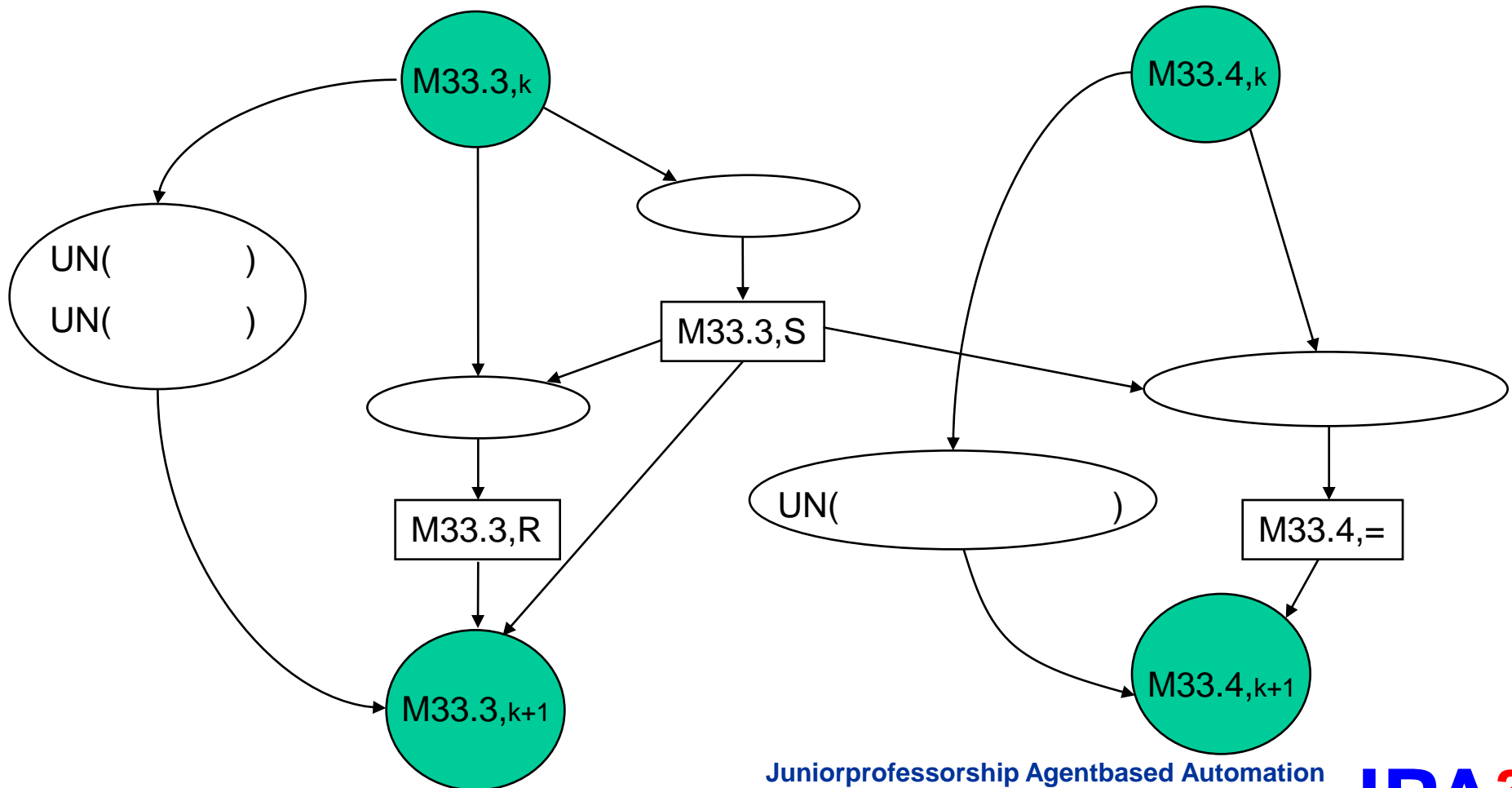
)

U E 13.6

S M 33.4



M33.3 S U M33.1	M33.3 R U M32.0	M33.4 = U E12.1 U M33.3
-----------------	-----------------	-------------------------



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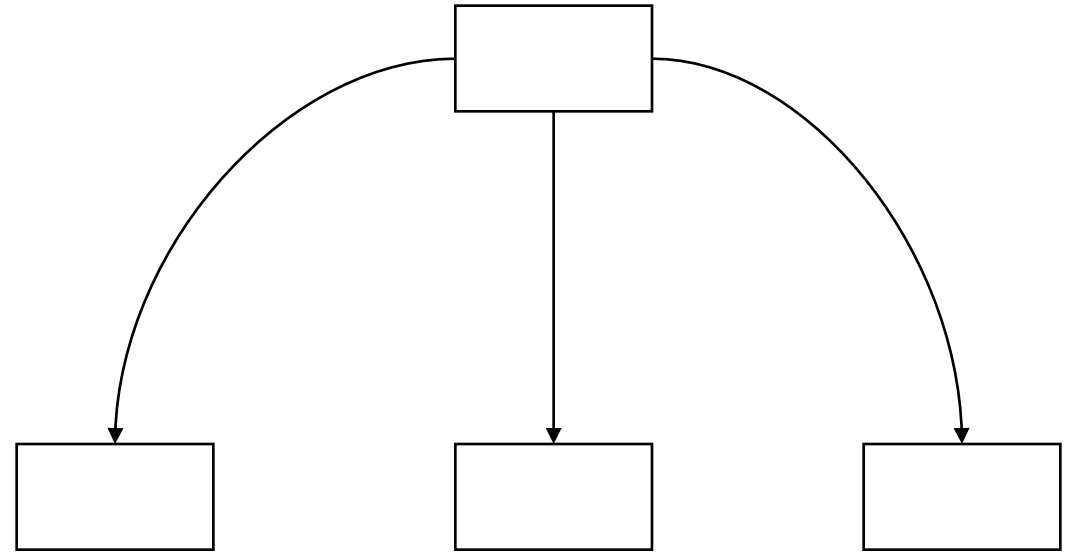
SW-Quality

Case Stud.

Summary

Outlook

OB 001
U M10.5
U A12.9
SPB PB 141
SPA FB 140
SPA FB 141



$$\Rightarrow m(G) = 0$$

→ Pure Tree Structure; easy Graph

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Summary

- μ_1 : number of distinct Operators
- μ_2 : number distinct Operands
- N_1 : total number of Operator occurrences
- N_2 : total number of Operands occurrences

$\mu = \mu_1 + \mu_2$: size of the vocabulary

$N = N_1 + N_2$: implementing length

Volume of the program: $V = N \log_2 \mu$

$$\Rightarrow \text{difficulty: } D = \frac{\mu_1}{2} \cdot \frac{N_2}{\mu_2} \quad \text{Effort: } E = V \cdot D$$

U; U(; O; O(; S; SI; SV; SE; SS; SA; ZV; ZR; !F;
><F; >F; >=F; <F; <=F; +F; -F; L; LC; T; R; =;)

Operators

E; A; M; T; Z

Operands

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Summary

- Flow graphs with e edges and n nodes:

$$v(G) = e - n + 2;$$

- Measure for linearly independent paths in G : $v(G) = d + 1$
- d : number of decisions in G
- Change on each operand from state K before the processing of the module to $K+1$ after processing
- Evaluation of the module after:

Value	Risk
1-10	An easy program, low risk
11-20	Complex program, endurable risk
21-50	Very Complex program, high risk
>50	Non testable program, extremely high risk

➤ This metric shows how easy/hard to test or maintain a given program or a module

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Summary

- Complexity determination of the calls between the blocks or modules
 1. Graph formation of the jumps
 - Starting point: current Block
 - End point : unconditional jump (**SPA**) or conditional jump (**SPB**) in current Block
 - Conditions for conditional jump are shown on the transitions
 2. Count edges (n) and nodes (e) of the Graph
 3. Calculate the Tree Impurity:

$$m(G) = \frac{2(e - n + 1)}{(n - 1)(n - 2)} \quad 0 \leq m(G) \leq 1$$

4. If the value tends to Zero this implies it is an easy graph

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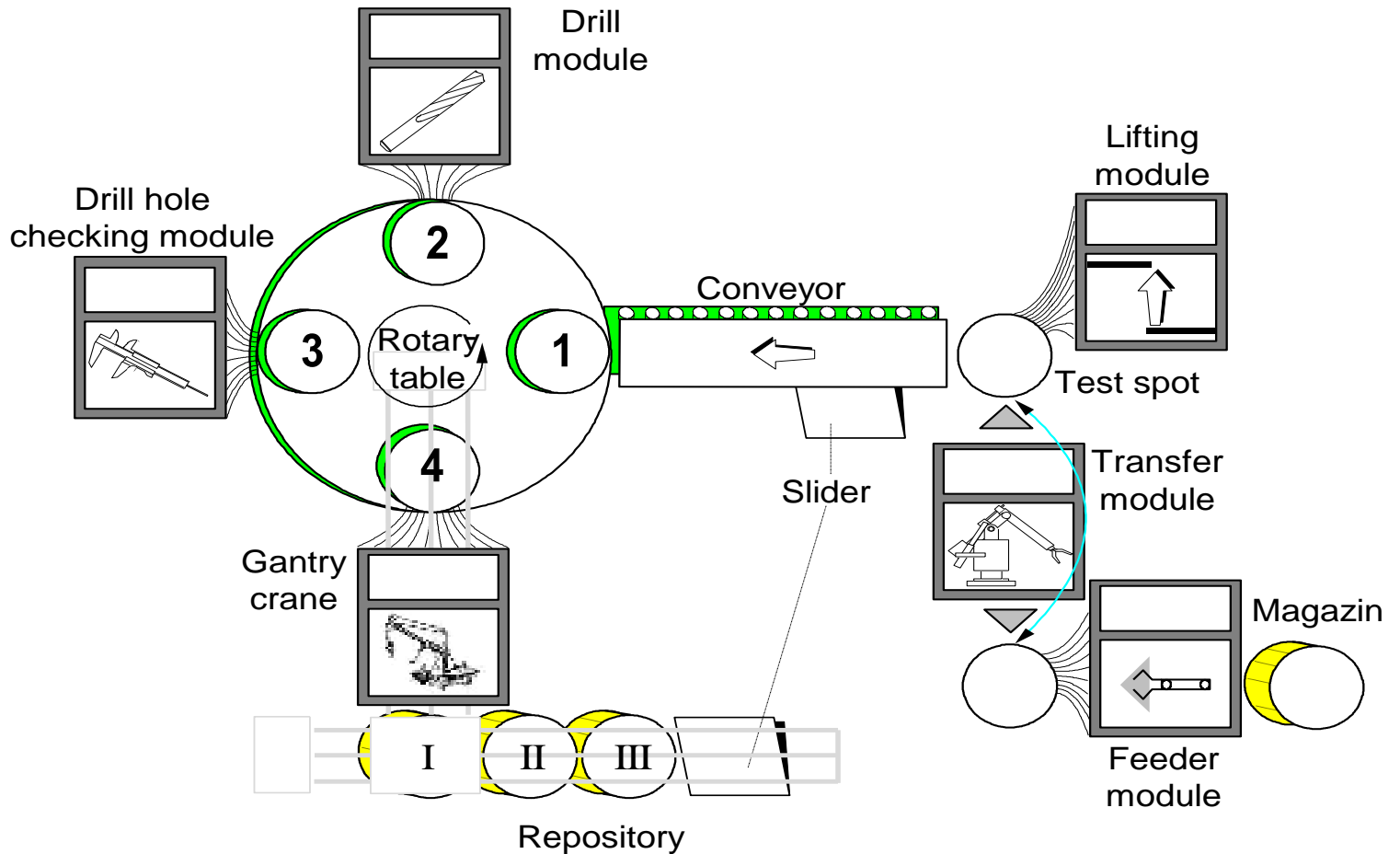
SW-Quality

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Summary

Description of the MPS (FESTO):

The task of this MPS is Sorting, processing, and Lifting of Cylindrical Pieces of different Materials



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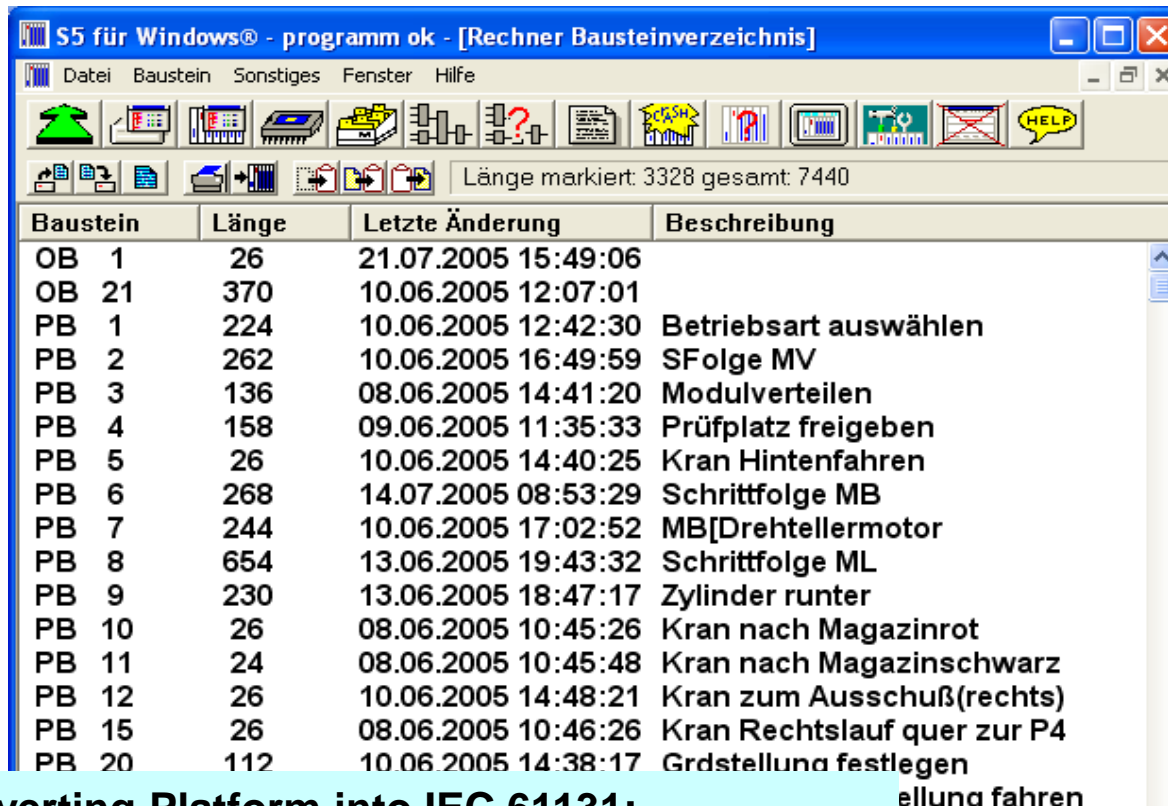
Visualization

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Baustein	Länge	Letzte Änderung	Beschreibung
OB 1	26	21.07.2005 15:49:06	
OB 21	370	10.06.2005 12:07:01	
PB 1	224	10.06.2005 12:42:30	Betriebsart auswählen
PB 2	262	10.06.2005 16:49:59	SFolge MV
PB 3	136	08.06.2005 14:41:20	Modulverteilen
PB 4	158	09.06.2005 11:35:33	Prüfplatz freigeben
PB 5	26	10.06.2005 14:40:25	Kran Hintenfahren
PB 6	268	14.07.2005 08:53:29	Schrittfolge MB
PB 7	244	10.06.2005 17:02:52	MB[Drehtellermotor
PB 8	654	13.06.2005 19:43:32	Schrittfolge ML
PB 9	230	13.06.2005 18:47:17	Zylinder runter
PB 10	26	08.06.2005 10:45:26	Kran nach Magazinrot
PB 11	24	08.06.2005 10:45:48	Kran nach Magazinschwarz
PB 12	26	10.06.2005 14:48:21	Kran zum Ausschuß(rechts)
PB 15	26	08.06.2005 10:46:26	Kran Rechtslauf quer zur P4
PB 20	112	10.06.2005 14:38:17	Grdstellung festlegen

Converting Platform into IEC 61131:

Symbol Table → Global variables

OB 1 → Program (Main)

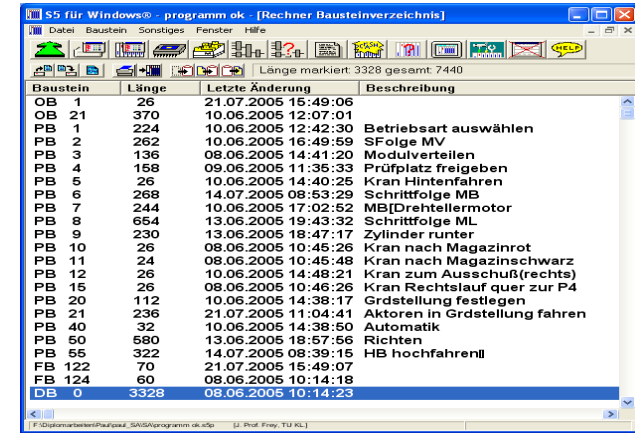
PBs → Function Block FBs

FBs → Function Block FBs with instance index

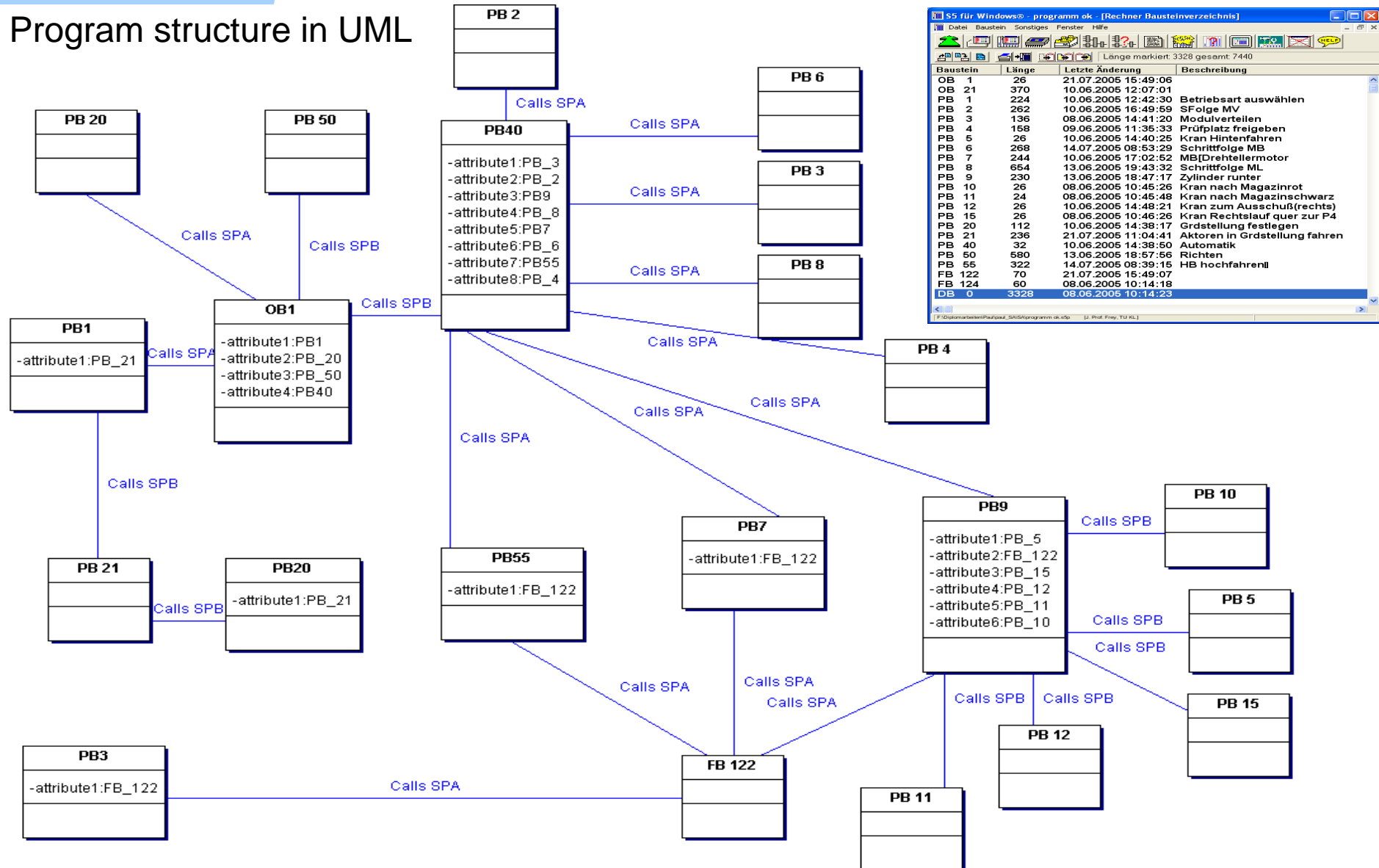
Blocks contains:

- Binary Operations
- Timer and Counters
- Non-Binary

Program structure in UML



Baustein	Länge	Letzte Änderung	Beschreibung
OB 1	26	21.07.2005 15:49:06	
OB 21	370	10.06.2005 12:07:01	
PB 1	224	10.06.2005 12:42:30	Betriebsart auswählen
PB 2	262	10.06.2005 16:49:59	SFolge MV
PB 3	136	08.06.2005 14:41:20	Modulverteilen
PB 4	158	09.06.2005 11:35:33	Prüfplatz freigeben
PB 5	26	10.06.2005 14:40:25	Kran Hintenfahren
PB 6	268	14.07.2005 08:53:29	Schrittfolge MB
PB 7	244	10.06.2005 17:02:52	MB[Drehtellermotor
PB 8	654	13.06.2005 19:43:32	Schrittfolge ML
PB 9	230	13.06.2005 18:47:17	Zylinder runter
PB 10	26	08.06.2005 10:45:26	Kran nach Magazinrot
PB 11	24	08.06.2005 10:45:48	Kran nach Magazinschwarz
PB 12	26	10.06.2005 14:48:21	Kran nach Ausschuß(rights)
PB 20	112	10.06.2005 14:38:17	Kran Rechtslauf quer zur P4
PB 21	236	21.07.2005 11:04:41	Grdstellung festlegen
PB 40	32	10.06.2005 14:38:50	Aktoren in Grdstellung fahren
PB 50	580	13.06.2005 18:57:56	Automatik
PB 55	322	14.07.2005 08:39:15	Richten
PB 122	70	21.07.2005 15:49:07	HB hochfahren!
FB 124	60	08.06.2005 10:14:18	
DB 0	3523	08.06.2005 10:14:26	



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Operand	Symbol	Kommentar
E 0.0	1K1	STEUERUNG AUS/EIN
E 0.2	1S10	LAMPENTEST
...
A 0.0	1H5	STEUERUNG
A 0.2	1H7	EINRICHTEN
...
M 0.0	M0.0	VKE = 0 FUER BCD WANDLUNG + VORZEICHEN
M 0.2	M0.2	RESET STOERMELDUNGEN
...
MB 120	MB120	STOERUNGEN S.WALZE FUER TEXTANZEIGE

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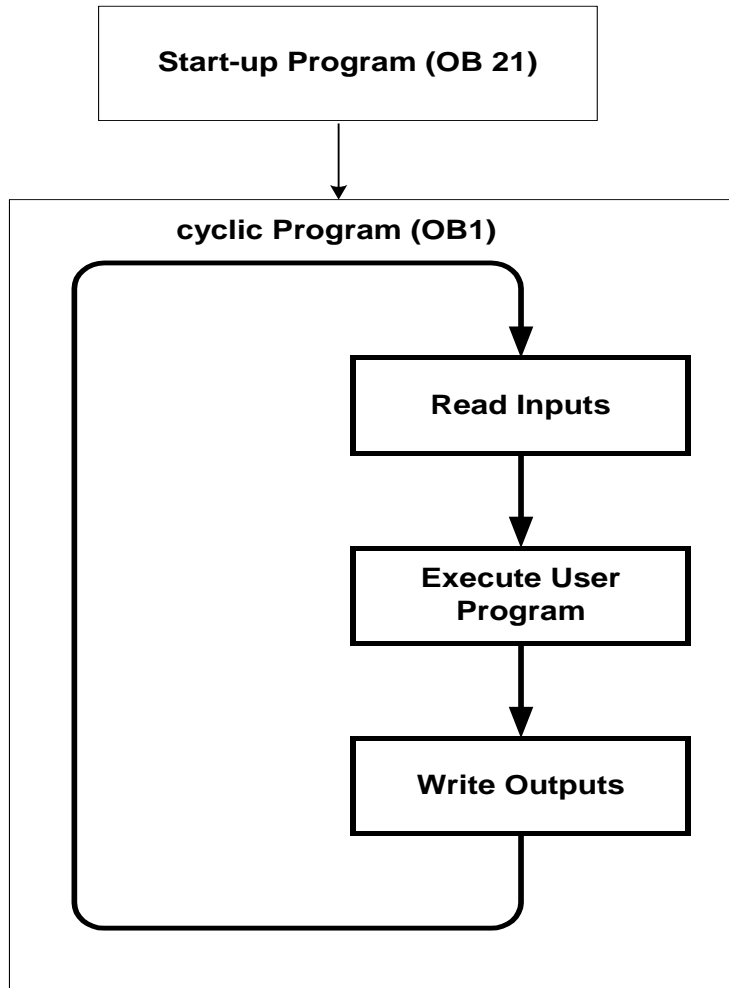
S5 Keywords in FSM
AND, ANDN, OR, ORN.

<, <=, >, >=, ><, =.

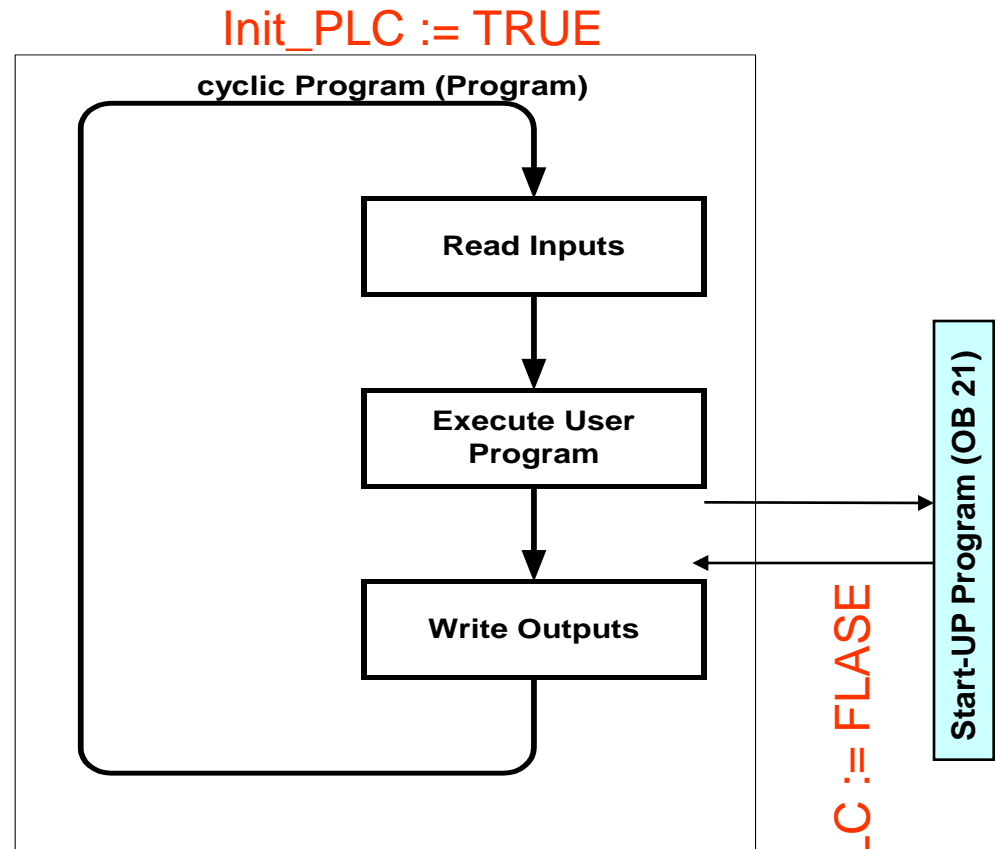
+, -, *, /.

Jump to, Call to.

S5 in FSM	IEC 61131-3
AND	AND
ANDN	ANDN
OR	OR
ORN	ORN
<, <=	LT, LE
>, >=	GT, GE
><	NE
=	=
+	ADD
-	SUB
*	MUL
/	DIV



STEP5



IEC 61131

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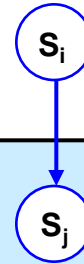
Summary

Outlook

- Binary Instructions

- Direct Converting of FSM (Mealy) into IEC 61131 (Logic und dynamic)
- Operanden are declared as Global Variables in IEC
- Variables from Symbol Table
- FSM Keywords → IEC Instructions

- Example



O: M 100.0= E 38.1 AND E 38.2 OR E 38.1
AND E 38.3 OR E 38.2 AND E 38.3

```
<?xml version="1.0" ?>
<fsm name="Pbonly_5b">
  <states>
    <state name="S0">
      <transition input="null" next="S1" action="M 100.0= E 38.1 AND E 38.2 OR E 38.1
AND E 38.3 OR E 38.2 AND E 38.3 " />
    </state>
    :
    :
  </states>
</fsm>
```

```
VAR
  M100_0: BOOL;
END_VAR
VAR_GLOBAL
  E38_2 AT IX38.2: BOOL;
  E38_1 AT IX38.1: BOOL;
  E38_3 AT IX38.3: BOOL;
END_VAR
```

```
S0: LD E38_1
AND E38_2
OR (True
AND E38_1
AND E38_3
)
OR (True
AND E38_2
AND E38_3
)
ST M100_0
JMP S1

S1:
```

IEC 61131

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Summary

Outlook

- Timer (T) and Counter (C) are
 - Not taken from FSMs (Logic)
 - Treated separately

SV → TP
SE → TON
SA → TOF
Reprogram other T and C types

Example: STEP 5

[3 Richten blinkt

```

UN    M 0.1
UN    M 0.2
U     M 80.0
UN    A 0.0
L     KT 003.2
SV    T 2
NOP   0
NOP   0
NOP   0
U     T 2
=     A 0.1
***

```

]

IEC 61131

```

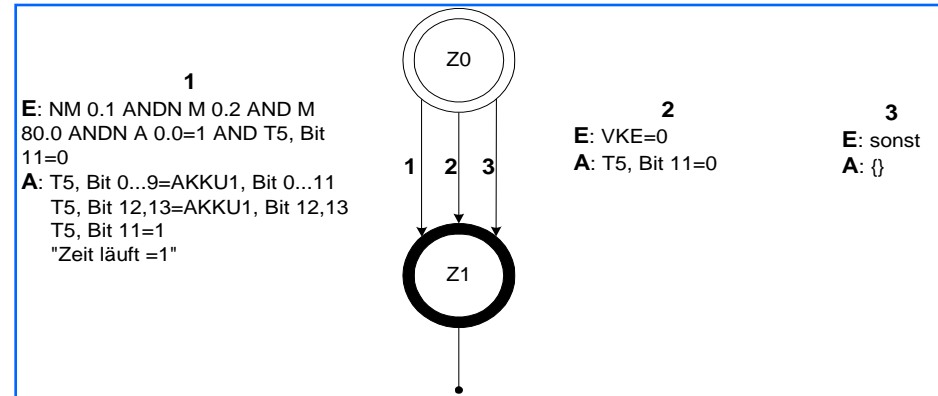
VAR
M0_1: BOOL;
M0_2: BOOL;
M80_0: BOOL;
T2: TP;
END_VAR
VAR_IN_OUT
A0_0: BOOL;
END_VAR
VAR_OUTPUT
A0_1: BOOL;
END_VAR

```

```

S0: LDN M0_1
ANDN M0_2
AND M80_0
ANDN A0_0
ST T2.IN
CAL T2 (PT :=
T#3000ms)
JMP S1
S1: LD T2.Q
ST A0_1

```



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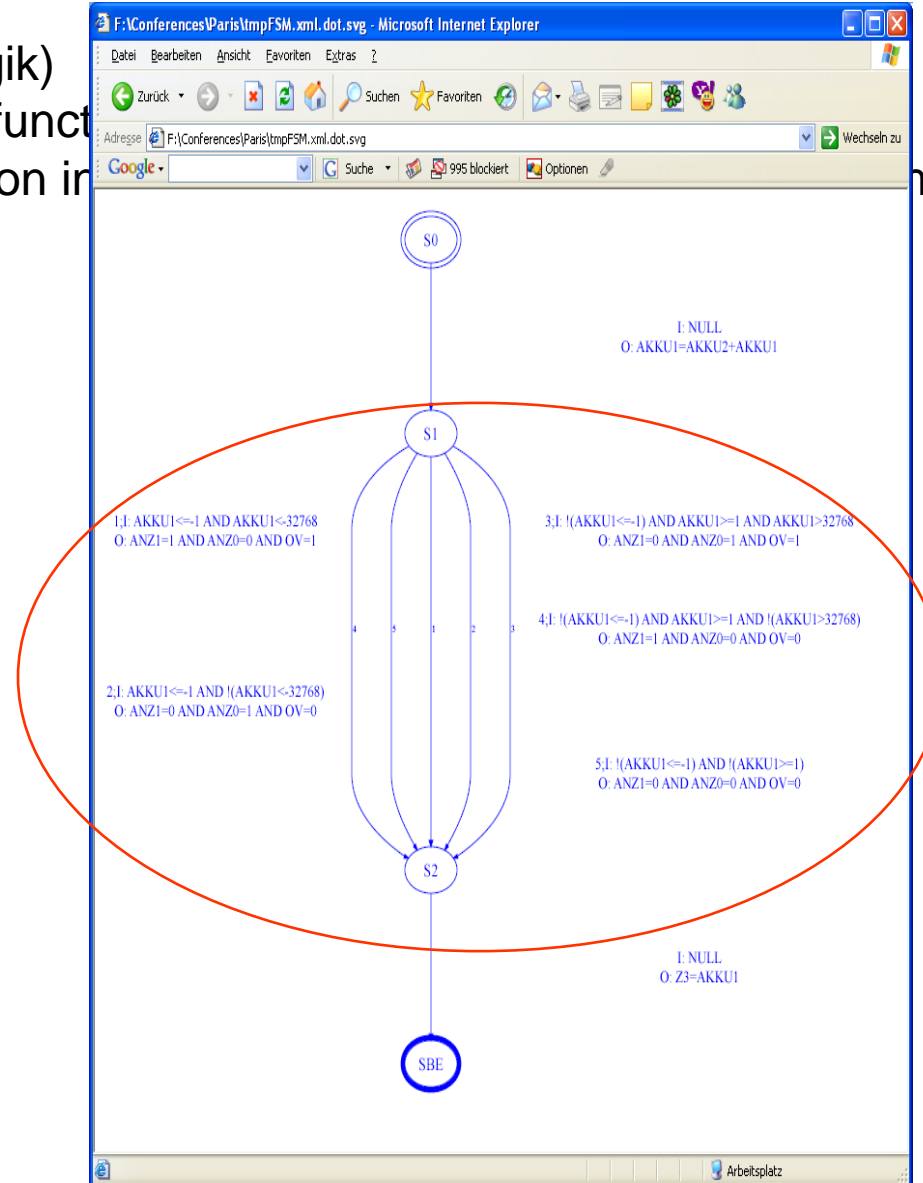
Summary

Outlook

- From the FSM (Logik)
- A new Function or funct
- non-binary instruction in

Example: STEP 5

[1			
NAME:	ADD		
BEZ :	Z1	EW	
BEZ :	Z2	EW	
BEZ :	Z3	AW	
	L	=Z1	
	L	KF +800	
	+F		
	T	=Z3	
	BE		
]			



- Transferred to an Array in the main as Global in the first use (Call)
- The corresponding Array index is changed in the after

```
PROGRAM MAIN
VAR_GLOBAL
DB2 :ARRAY [0..255] OF
DINT:= [0,128,130,1.....
```

IEC 61131

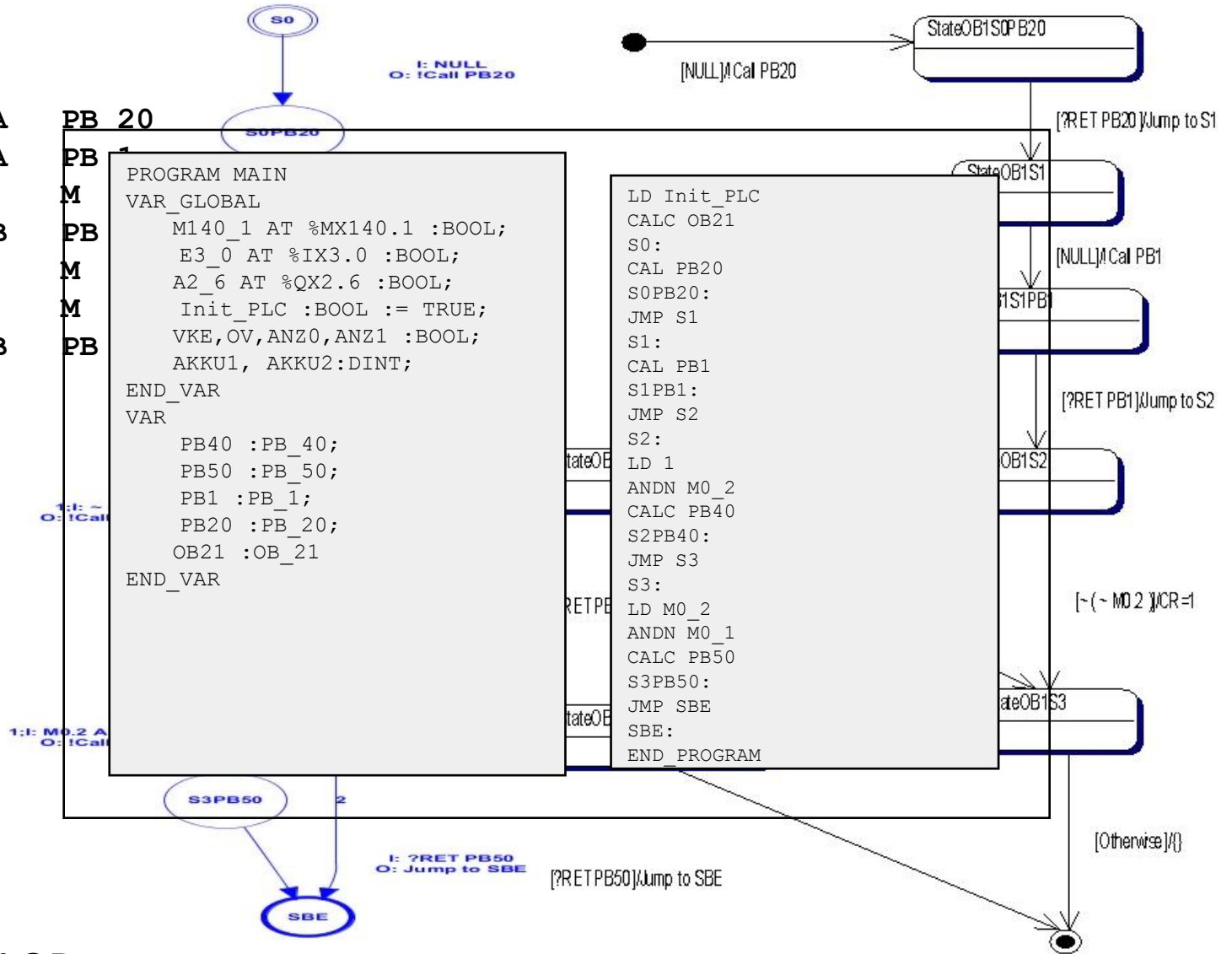
Example: STEP 5 (PB 1)

```
[1
      A          DB 2
      SPA        FB 2
NAME:  ADD
Z1  :   DW 3
Z2  :   DW 4
Z3  :   DW 5
      L          DW 5
      T          MW 10
      BE
]
```

```
FUNCTION_BLOCK PB_1
VAR_EXTERNAL
  DB2 :ARRAY [0..255] OF DINT;
  MW10 :DINT;
END_VAR
VAR
  FB2_1 :FB_2;
END_VAR
S0:
(*Call to DB2*)
S1:
CAL
FB2_1 (Z1:=DB2 [3], Z2:=DB2 [4] | DB2 [5]
]:=Z3)
S1FB2:
JMP S2
S2:
LD DB2 [5]
ST MW10
SBE:
END_FUNCTION_BLOCK
```

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[1
SPA
SPA
UN
M
SPB
U
M
UN
M
SPB
PB
BE
]



Conversion of OB1

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Summary

Block	LOC (NCSS)	Block	LOC (NCSS)
FB122	8	PB3	20
OB1	8	PB4	56
OB21	177	PB40	9
PB1	72	PB5	6
PB10	6	PB50	209
PB11	5	PB55	99
PB12	6	PB6	97
PB15	6	PB7	70
PB2	104	PB8	261
PB20	40	PB9	56
PB21	81	total NCSS: 1403	

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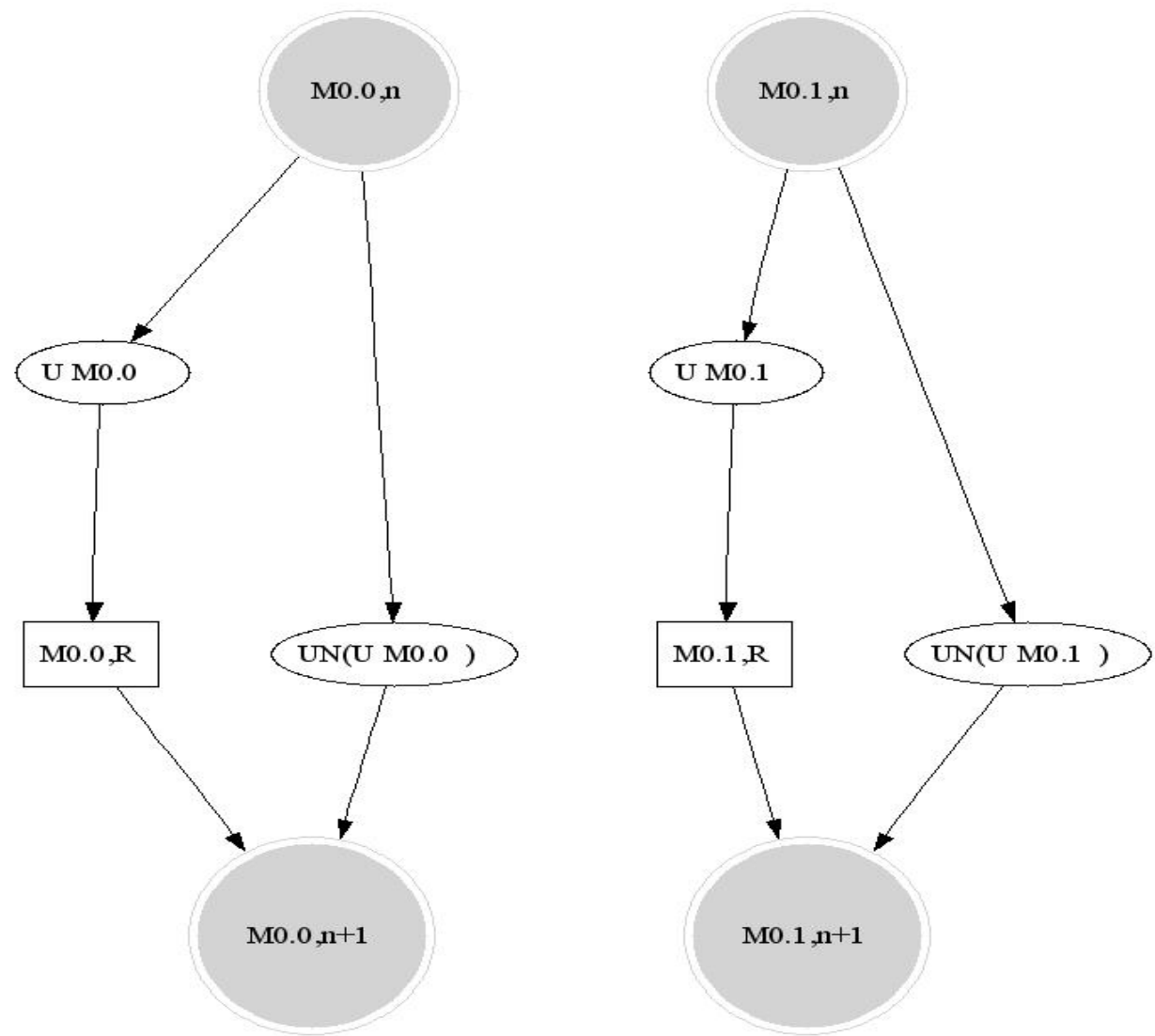
SW-Quality

Case Stud.

Summary

Block	Volume	Difficulty	Effort
FB122	0	0	0
OB1	0	0	0
OB21	2864	1	2864
PB1	828	8	6624
PB10	32	2	64
PB11	22	2	44
PB12	32	2	64
PB15	32	2	64
PB2	998	15	14970
PB20	357	2	714
PB21	1237	8	9896
PB3	104	1	104
PB4	495	9	4455
PB40	0	0	0
PB5	32	2	64
PB50	3281	40	131240
PB55	862	15	12930
PB6	1261	12	15132
PB7	673	6	4038
PB8	3363	20	67260
PB9	390	4	1560
Average	937	8	15115

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OB 21 Segment

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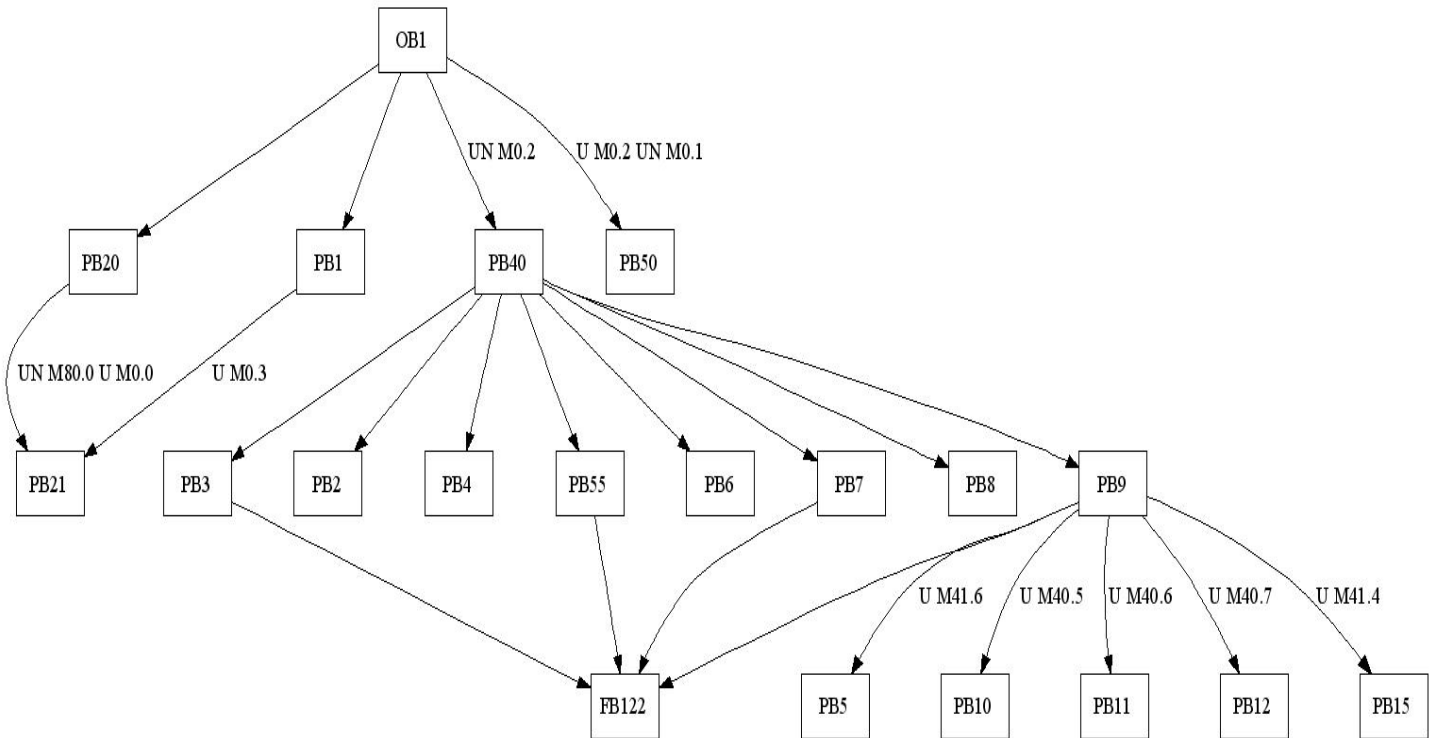
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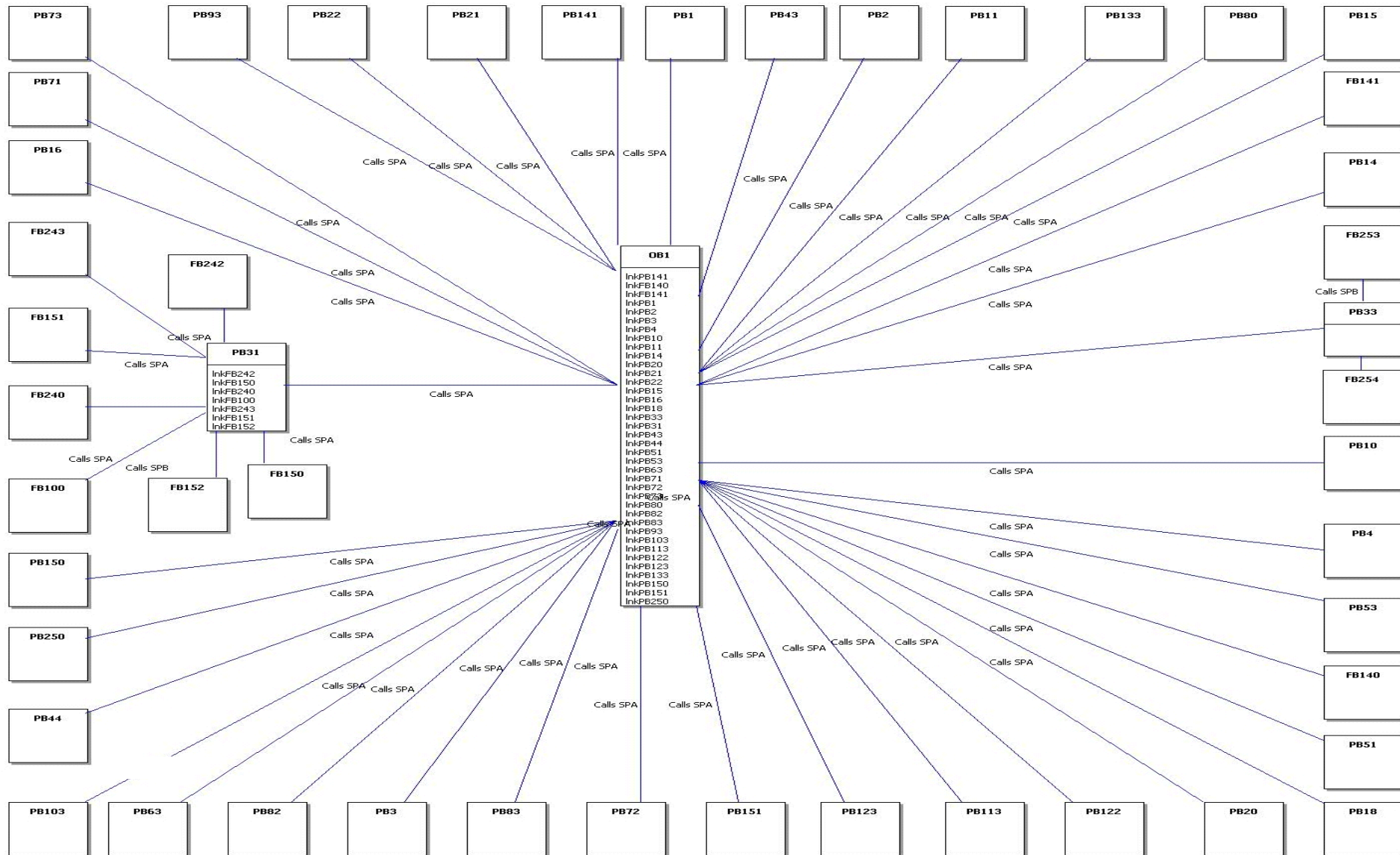
Tree Impurity = 0.023391813

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Freudenberg (PK14)

Main goal was the
diagnosability

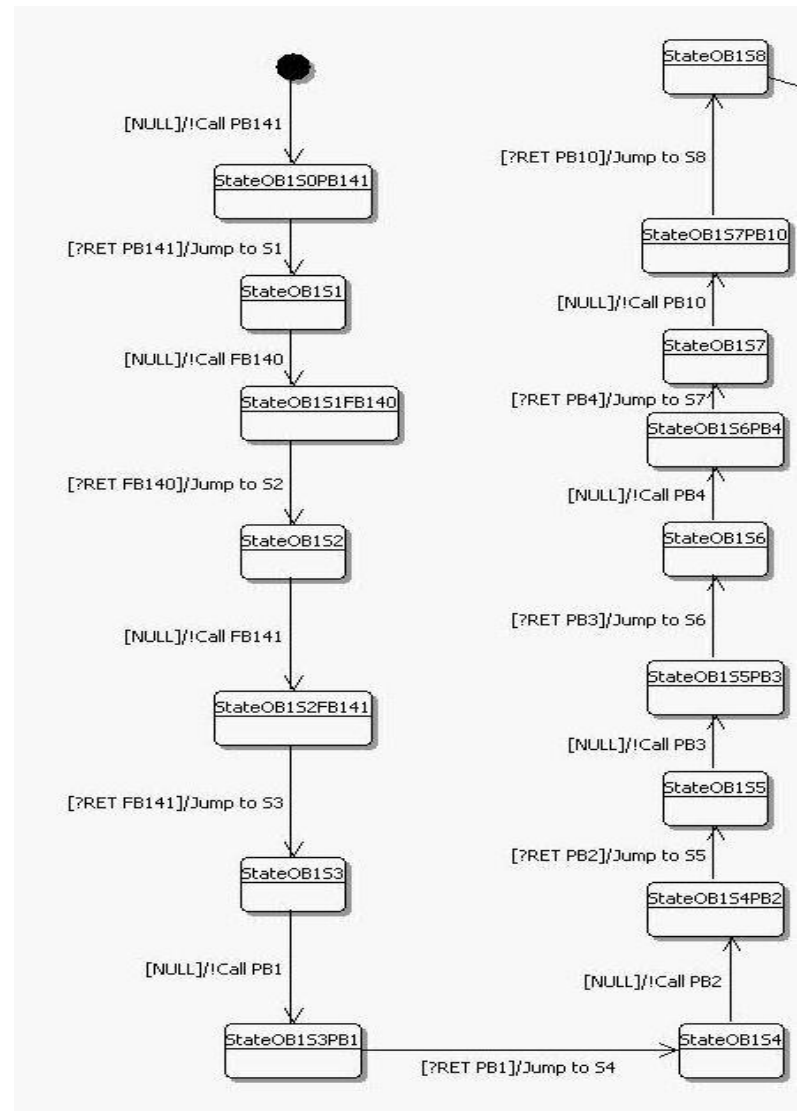
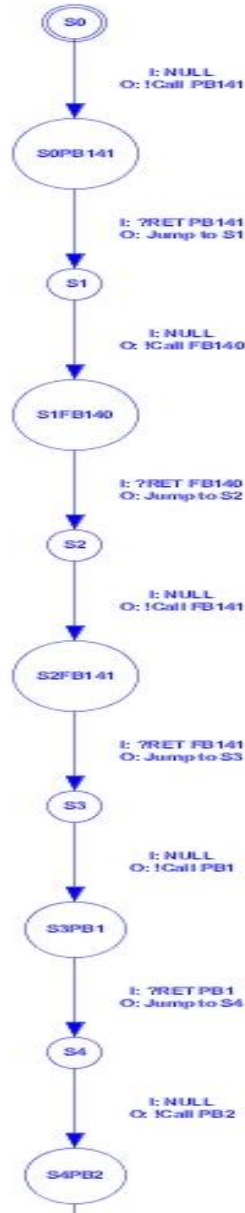




Program structure in UML

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Conversion of
OB1 segment



Block	NCSS	Block	NCSS	Block	NCSS	Block	NCSS
FB100	3	FB101	3	PB113	15	PB122	131
FB140	10	FB141	10	PB123	46	PB133	55
FB150	10	FB151	6	PB14	386	PB141	76
FB152	6	FB153	63	PB15	57	PB150	62
FB154	21	FB240	2	PB151	30	PB16	314
FB241	2	FB242	2	PB18	173	PB19	1
FB243	2	FB244	2	PB2	50	PB20	93
FB245	2	FB246	2	PB21	179	PB22	79
FB247	2	FB248	2	PB250	479	PB251	13
FB249	2	FB250	2	PB252	5	PB3	43
FB251	2	FB252	27	PB31	113	PB33	34
FB253	14	FB254	29	PB4	17	PB43	39
FB255	30	OB1	39	PB44	39	PB51	18
OB13	2	OB21	3	PB53	8	PB63	80
OB22	3	OB31	2	PB71	20	PB72	24
PB1	36	PB10	209	PB73	63	PB80	62
PB103	43	PB11	23	PB82	20	PB83	34
PB93	19	total NCSS 3493					

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Block	Volume	Difficulty	Effort	Block	Volume	Difficulty	Effort
FB140	36.0	6.0	216.0	PB16	3847.0	18.0	69246.0
FB141	36.0	6.0	216.0	PB18	1939.0	15.0	29085.0
PB1	337.0	5.0	1685.0	PB2	456.0	4.0	1824.0
PB10	2246.0	16.0	35936.0	PB20	801.0	10.0	8010.0
PB103	342.0	2.0	684.0	PB21	2077.0	9.0	18693.0
PB11	172.0	4.0	688.0	PB22	656.0	2.0	1312.0
PB113	91.0	2.0	182.0	PB250	6648.0	14.0	93072.0
PB122	1381.0	15.0	20715.0	PB3	321.0	3.0	963.0
PB123	407.0	3.0	1221.0	PB31	899.0	7.0	6293.0
PB133	677.0	3.0	2031.0	PB33	221.0	6.0	1326.0
PB14	4398.0	30.0	131940.0	PB4	143.0	3.0	429.0
PB141	657.0	1.0	657.0	PB43	296.0	5.0	1480.0
PB15	549.0	8.0	4392.0	PB44	296.0	5.0	1480.0
PB150	540.0	10.0	5400.0	PB51	135.0	8.0	1080.0
PB151	253.0	4.0	1012.0	PB53	42.0	3.0	126.0
PB80	564.0	12.0	6768.0	PB63	792.0	5.0	3960.0
PB82	154.0	3.0	462.0	PB71	167.0	3.0	501.0
PB83	265.0	4.0	1060.0	PB72	188.0	3.0	564.0
PB93	131.0	2.0	262.0	PB73	585.0	4.0	2340.0
Average	888.03	6.92	12034.5				

Block	Value	Risk	Block	Value	Risk
FB140	2	easy Program, low Risk	PB16	60	untestable Program, extremely high Risk
PB10	38	Very Complex Program, High Risk	PB18	44	Very Complex Program, High Risk
PB44	9	easy Program, low Risk	PB2	14	Complex Program, endurable Risk
PB4	8	easy Program, low Risk	PB20	11	Complex Program, endurable Risk
PB103	2	easy Program, low Risk	PB21	6	easy Program, low Risk
PB11	9	easy Program, low Risk	PB22	2	easy Program, low Risk
PB113	2	easy Program, low Risk	PB3	2	easy Program, low Risk
PB122	20	Very Complex Program, High Risk	PB250	132	untestable Program, extremely high Risk
PB123	2	easy Program, low Risk	PB31	18	Complex Program, endurable Risk
PB133	6	easy Program, low Risk	PB33	15	Complex Program, endurable Risk
PB14	55	untestable Program, extremely high Risk	PB141	64	untestable Program, extremely high Risk
FB141	2	easy Program, low Risk	PB43	9	easy Program, low Risk
PB15	12	Complex Program, endurable Risk	PB80	14	Complex Program, endurable Risk
PB150	3	easy Program, low Risk	PB51	8	easy Program, low Risk
PB151	5	easy Program, low Risk	PB53	2	easy Program, low Risk
PB1	10	Complex Program, endurable Risk	PB63	10	Complex Program, endurable Risk
PB82	5	easy Program, low Risk	PB71	5	easy Program, low Risk
PB83	5	easy Program, low Risk	PB72	7	easy Program, low Risk
PB93	2	easy Program, low Risk	PB73	5	easy Program, low Risk

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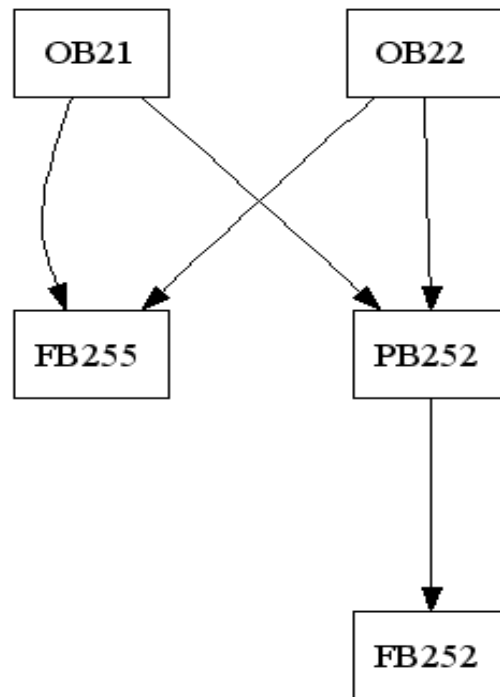
SW-Quality

Case Stud.

Summary

Tree Impurity = $-6.4935064E-4$

→ The negative value makes it clear that the graph of the tree impurity consists of more than one tree structure.



Tree Impurity segment of PK14



- © Re-Eng. of PLC programs requires a Model
- © PLC program were modeled as CFSMs
- © PLC code was transformed to FSM after the optimization using IF-THEN-ELSE
- © UML and XML made it possible to get a model of the PLC
- © Re-implementation of the existing PLCs from the existing structure and formal description → IEC 61131
- © SW Quality derivation of the PLC program



Oops clicked firmly 😊

Additional Slides

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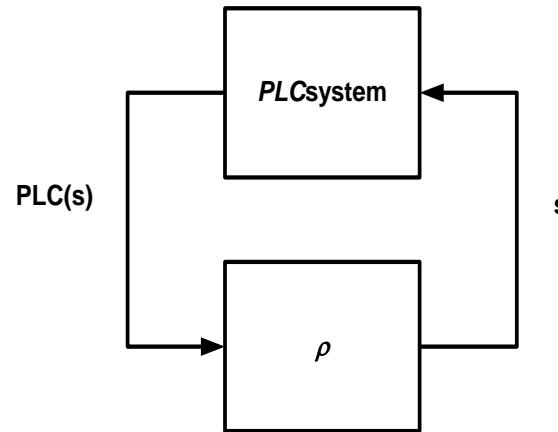
Re-Implem.

SW-Quality

Case Stud.

Summary

- $PLC_{system}/\rho \rightarrow Closed\ loop$



plant as a FSM $\rho = \langle X, \Sigma, X_0, X_f, \delta \rangle$ where

- X Finite set of states
- $X_0 \subseteq X$ set of initial states
- $X_f \subseteq X$ set of final states also marked or accepted) states of ρ
- Σ finite alphabet of ρ
- δ partial transition function mapping $X \times \Sigma$ to X
 $\rightarrow \delta(x_i, e)$ an event $e \in \Sigma$ leads $x_i \in X$ to state $x_j \in X$

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Summary

- PLC_{system} as a tuple $\langle PLC_{SW}, PLC_{HW}, PLC_{Cycle} \rangle$
- PLC_{SW} PLC program as tuple

$$\langle PAE, PAA, I, A_{PAE}, PLC_{pr}, x_0, x_f \rangle$$

- PAE non empty finite ordered set of binary inputs
- PAA non empty finite ordered set of binary outputs
- I non empty finite ordered set of binary internal variables of PLC
- $\alpha(I)$ as Cartesian product $\{0, 1\}^{|I|}$ which is the alphabet generated by the nonempty ordered set of variables I
- PLC_{pr} is the PLC program described as a partial function

$$PLC_{pr}(x, e) : \alpha(I) \times \alpha(PAA) \times A_{PAE} \rightarrow \alpha(I) \times \alpha(PAA)$$

where $x \in \alpha(A_{PAE}) \times \alpha(PAA)$ and $e \in A_{PAE}$ and x_0 , an initial state of the PLC program such that $x_0 \in \alpha(I) \times \alpha(PAA) = \{0, 1\}^{|I|+|PAA|}$

- $A_{PAE} \not\subseteq \mathcal{D}(PAE)$ of recognized inputs

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Summary

- PLC_M Module or Block as a stand alone is a tuple $\langle S, \Sigma, Y, \delta, \lambda, s_0, s_f \rangle$
- S set of states
- $\Sigma = \alpha(PAE)$ input alphabet
- $b \in Binary$ range over binary variables
- $bexpr$ is derived which ranges over Boolean expressions
- $bexpr \in Bexpr+$ where $Bexpr+$ is the language generated by $Gexpr$ grammar

$$Gexpr = 1|0|b|\sim b|\sim(Gexpr)$$

$$| (Gexpr \wedge Gexpr) | (Gexpr \vee Gexpr)$$

$$| (Gexpr \equiv Gexpr) | (Gexpr * Gexpr)$$

→ $Gexpr$ is also an alphabet since Δ  are called closed binary on $pow(v)$ where v is the universe

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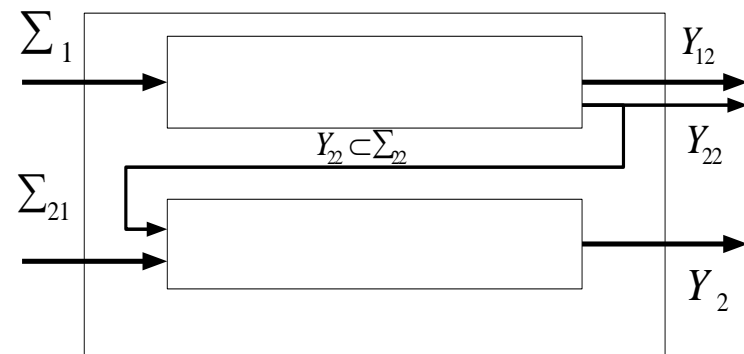
SW-Quality

Case Stud.

Summary

- PLC_{SW} is a two subsets PLC_u and PLC_{SYS}
- PLC_u is Re-engineering relevant
- PLC_u is a model of CFSM $PLC_{M1} \dots PLC_{Mn}$ of $\langle S_i, \Sigma_i, Y_i, \delta_i, \lambda_i, s_{0,i} \rangle$
- The model $PLC_{Mi} \forall i \in \{1, \dots, n\} PLC_{M1} \otimes PLC_{M2} \dots \otimes PLC_{Mn}$ builds the automaton $PLCu := \uparrow S, \bullet, Y, \delta, \lambda, s_0 \hat{\uparrow}$ such that in case of no Sync.

General feed-forward composition

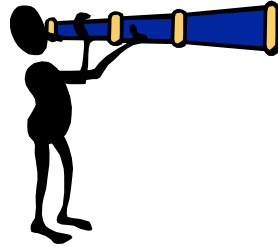


$$Y_i = Y_{i1} \times Y_{i2}$$

$$\Sigma_i = \Sigma_{i1} \times \Sigma_{i2}$$

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- ⇒ Implementation of the UML Activity diagrams
- ⇒ Application of the method to other PLC proprietary languages
- ⇒ Re-Implementation into new Systems (IEC 61499)
- ⇒ Extension of the SWQ to the dynamic of the PLC program

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Summary

- Size Metric

- Lines of Code (LOC)
- Non-Commented Source Statements (NCSS)

- Halstead-Measure

- Calculation through operands and operators of:
 - implementing length
 - size of the vocabulary
 - Volume of the program
 - Difficulty and Effort

- McCabe Cyclomatic Complexity Measure

- Calculation through Flow graph with e edges and n nodes:
 $v(G)=e-n+2$;

- Tree Impurity:
$$m(G) = \frac{2(e - n + 1)}{(n - 1)(n - 2)} \quad 0 \leq m(G) \leq 1$$

➤ If the value tends to zero, this implies it is an easy graph